



Colloidal Systems

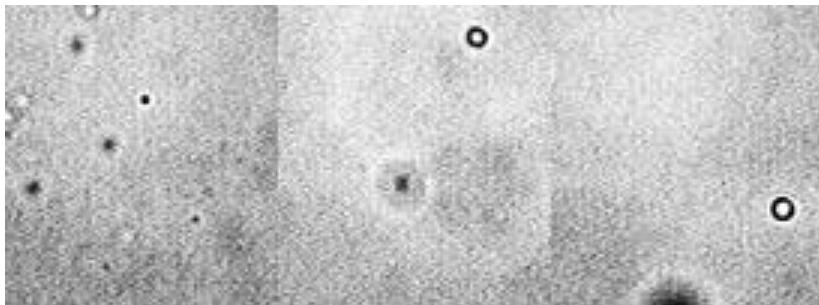
(Lecture 1)



George Petekidis

**IESL-FORTH & Department of Materials Science
and Technology, University of Crete, Heraklion,
Crete, Greece**

georgp@iesl.forth.gr



IoP, Durham, April 2017



Colloidal systems



Outline:

- **Examples-Applications**
- **Main phenomena - Forces - Time scales**
- **Phase behavior: Thermodynamic phases, Metastable states (glasses and gels)**
- **Microscopic Dynamics (Scattering-Microscopy)**
- Mechanical properties (Rheology) -> 2nd lect.
- Rheology of suspensions and glasses -> 2nd lect.
- Rheology of attractive colloids and gels -> 3rd lect.



Colloidal systems



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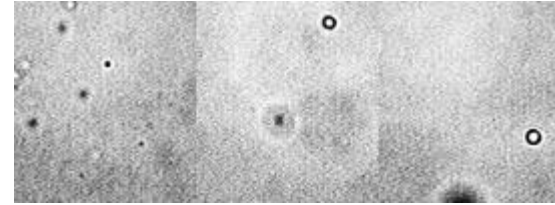
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- Mechanical properties (Rheology)



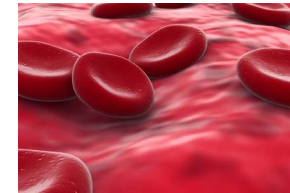
Colloids –Examples



Example: Particles with size few nm to few μm suspended in a liquid



Paints, Inks, lubricants, shampoo, foodstuff, blood, ...



Biological systems and applications:
Protein crystallisation,
macromolecular crowding
in biological cells, drug
release, etc

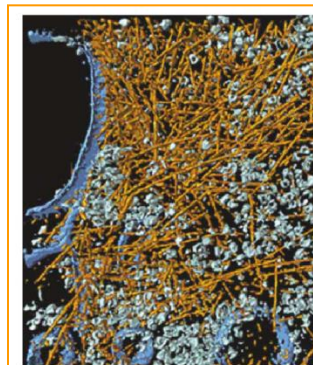


Figure 1 Crowded interior. This three-dimensional reconstruction shows part of the cytoplasm of an intact mottle *Dicyostelium discoideum* cell. The orange linear complexes are actin filaments; ribosomes and other macromolecular complexes are in grey; membranes are in blue. Reprinted with permission from ref. 3.

biomaterials





Colloidal Systems



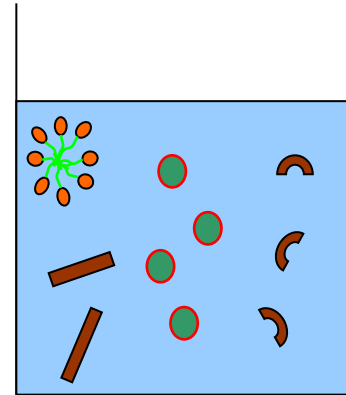
Which systems are colloidal?

General Definition: Two immiscible component mixtures

Dispersed phase (gas, liquid, solid) in suspending medium (gas, liquid, solid)

Size of dispersed particles: ~ 10 nm to ~ 5 μ m

Brownian motion keeps $\Rightarrow k_B T > m_B g R$
them from sinking $\Rightarrow \text{radius } R \leq 1 - 5 \mu\text{m}$



Examples:

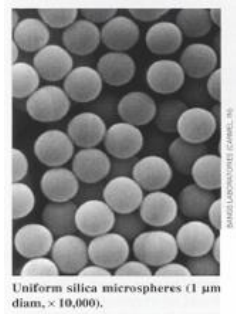
Solid particles suspended in a liquid (paints, blood, milk ...)

Liquid particles in a liquid medium (emulsions,...)

Solid particles in gas (aerosols,...)

Gas in liquid (foams,...).... etc.. ..

all combinations .. but one.



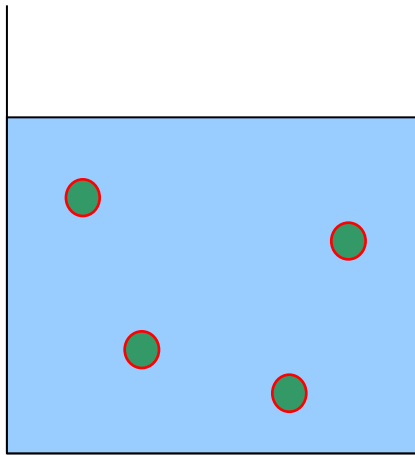


Colloidal Systems

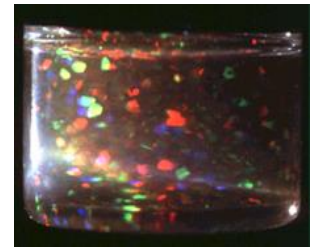
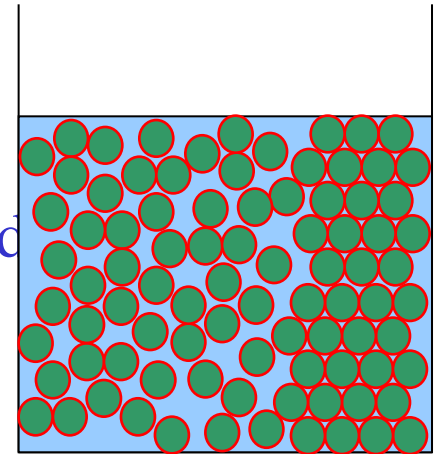


States: Liquids, Crystals, Glasses, Gels

Dilute:
Colloidal
“gas”



Concentrated:
Colloidal liquid
or solid

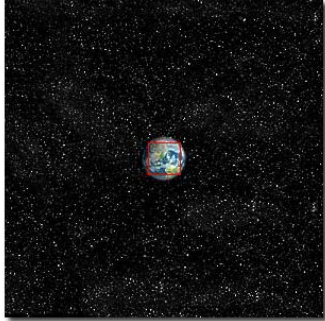




The middle world: Mesoscopic phenomena



The Earth from 100,000 Kilometers.



10^8 meters 100,000 kilometers

Top of large Oak tree.



10^1 meters 10 meters

Oak tree branch with leaves.



10^0 meters 1 meter

Surface of an Oak leaf magnified 10 times.



10^{-2} meters 1 centimeter

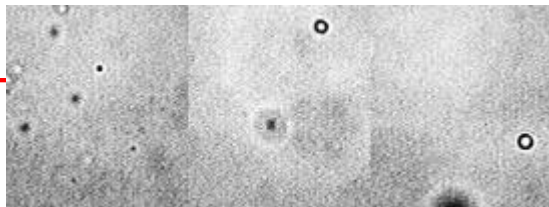
Macro - world

Brownian Motion : “The restless heart of matter and life”
M.D. Haw



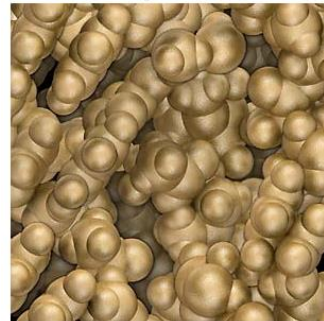
0 nanometers

Middle – world
10 nm – 10 μ m



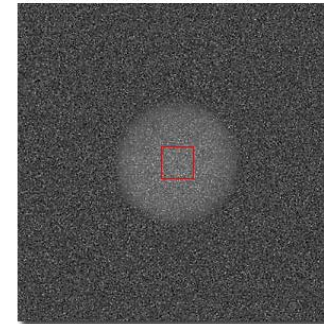
atomic world

DNA nucleotide building blocks.



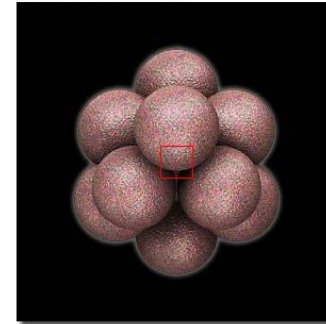
10^{-9} meters 1 nanometer

Outer electron cloud of a carbon atom.



10^{-10} meters 100 picometers

Nucleus of the carbon atom.



10^{-14} meters 10 femtometers



Colloidal Suspensions as model mesoscopic systems



“Colloids as large atoms” (P. N. Pusey)

- Collection of interacting particles – can tune interactions
- Can reach thermodynamic equilibrium – colloidal gases, liquids and solids
- Can be trapped in metastable, non-ergodic states– glasses, gels
 - Can study phenomena of generic interest:
crystallization, glass formation and melting, ageing etc.

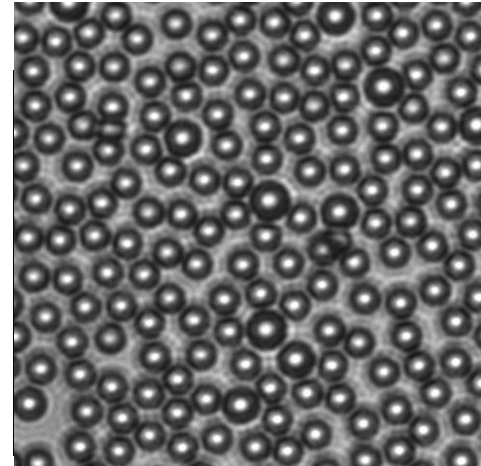
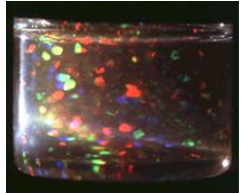
Colloidal solids are weak and “slow”



Model Systems: Hard-sphere colloids



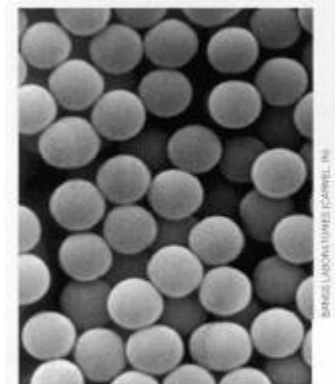
Sterically-stabilised poly-methylmethacrylate (PMMA) colloidal “hard spheres”



- Suspend in mixture of organic liquids –
nearly transparent samples even at high concentrations
- No attraction, nearly hard-sphere repulsion
- Radius $R \approx 0.2$ to $1 \mu\text{m}$

“Plastic Brownian billiard balls”

Other “hard” spheres: Silica particles (small steric layer, PS particles (charged stabilized + salt to screen interactions))



Uniform silica microspheres (1 μm diam, $\times 10,000$).



Colloids as “Large Atoms”



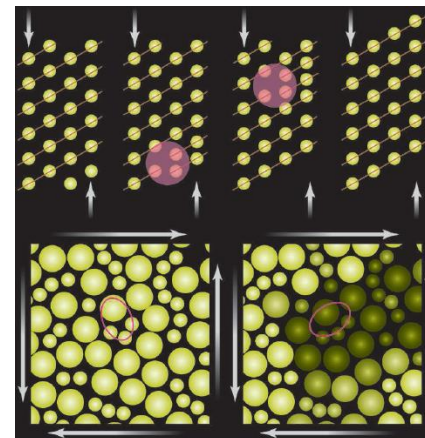
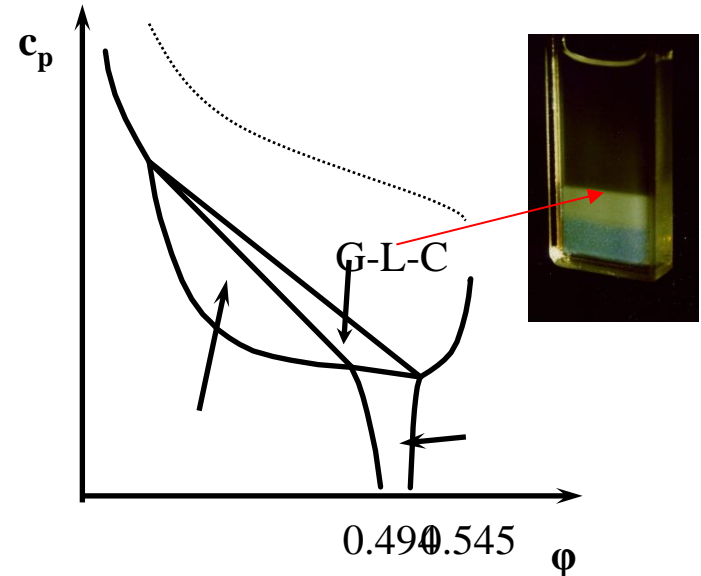
Phase behavior

Dynamics of Crystallization

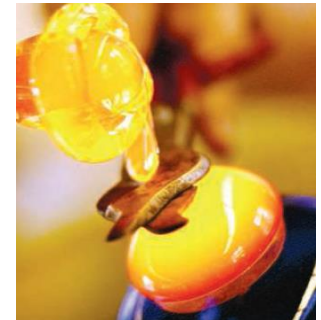
Non-ergodic states (glasses, gels)

Flow of glassy and crystalline
molecular systems

Metallic glasses



The role of defects. (Top) In crystals, flow is determined by dislocations,

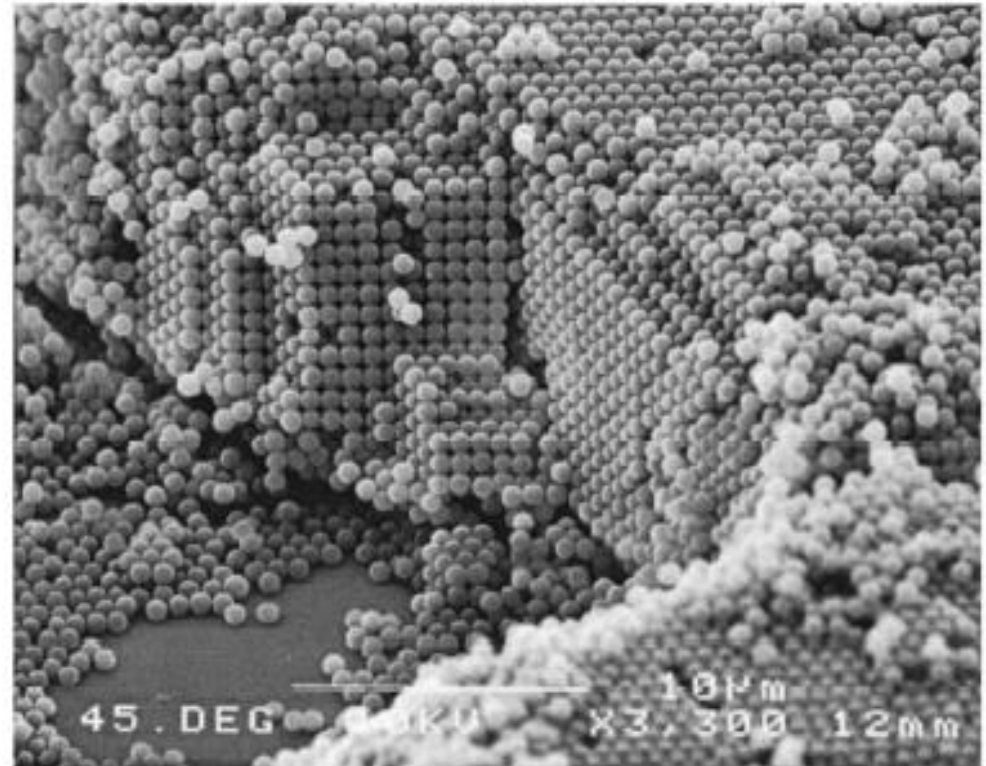




Applications - Why are colloids interesting ?



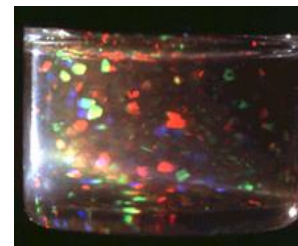
Scanning electron microscope pictures of dried sample



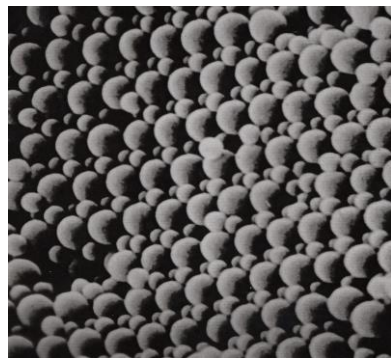
(b)

Shear induced hard-Sphere FCC Crystal

R.M. Amos et al.,
PRE **61**, 2929
(2000)



Binary Colloidal Crystal
 AB_2 $R_B/R_A = 0.58$



- “Colloid engineering”

New materials, e.g. photonic or phononic crystals from colloidal precursors

high precision filters, controlled porosity substrates from colloidal precursors.

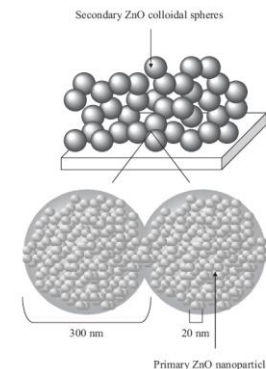


More applications of colloidal systems



- **Nanocomposites (colloids in polymeric matrices) photovoltaics and other applications**

- **Magnetic particles in 2D, Magneto-rheological fluids**



Chu et al. *Adv. Materials*, 2007

- **Optofluidics (flow induced structures for optical applications)**

NATURE|Vol 442|27 July 2006|doi:10.1038/nature05060

Developing optofluidic technology through the fusion of microfluidics and optics

Demetri Psaltis¹, Stephen R. Quake² & Changhuei Yang¹

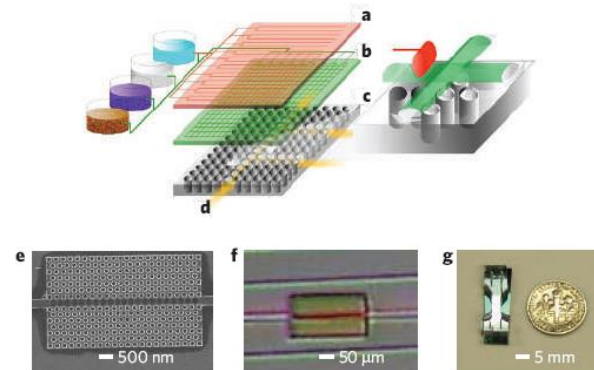
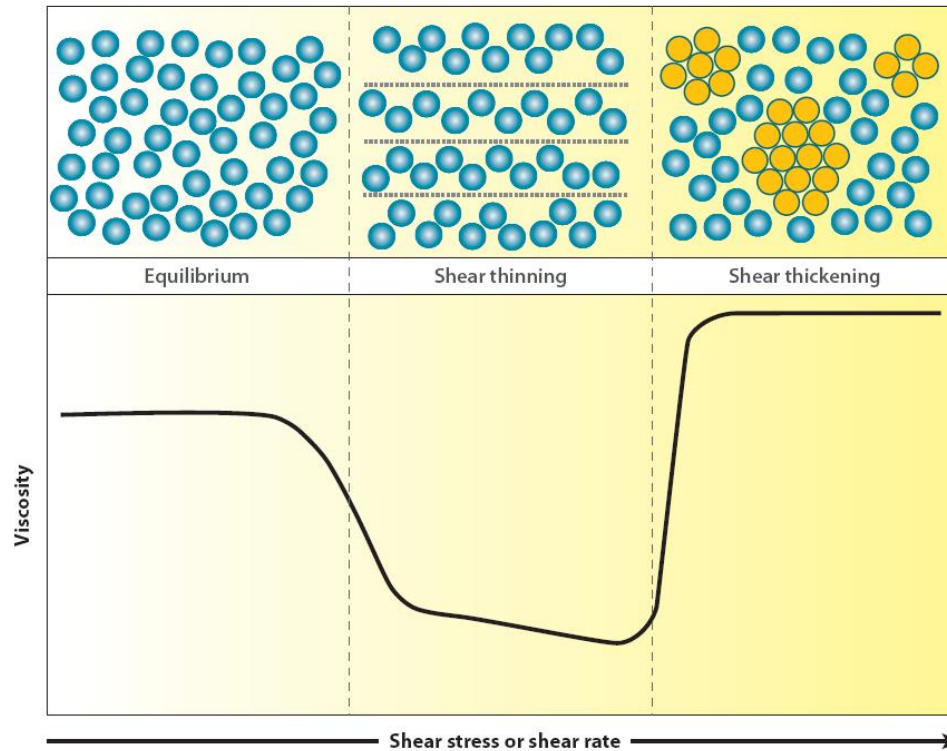


Figure 1 | A generalized layer construction of an optofluidic device. An



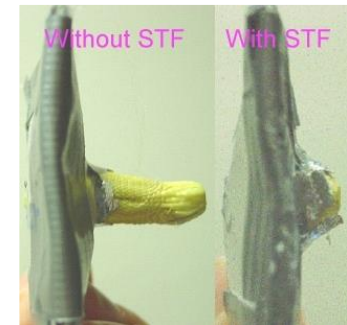
Applications: Rich Flow properties (colloids, grains, emulsions, etc)



Wagner and Brady

Non-Newtonian fluids: thixotropy - rheopexy

Applications of shear thickening



Liquid Armor

Wagner, (Delaware)



<http://www.youtube.com/watch?v=f2XQ97XHjVw>



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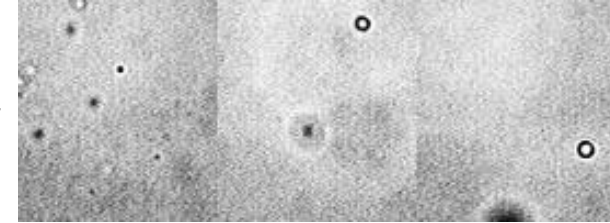


Main phenomena – Brownian motion

Mean square displacement of a particle of radius R

$$\langle \Delta r(t)^2 \rangle = 6Dt \quad \text{Einstein-Smoluchowski (1905), for } t > t_B = \frac{m}{6\pi\eta R}$$

$$D_0 = \frac{k_B T}{6\pi\eta R} \quad \text{Stokes-Einstein-Sutherland diffusion coefficient}$$



for colloids time to diffuse their own radius : $t \approx 1\text{ms} \dots 1\text{s}$

Large particles => Slow diffusion

J. Perrin (Nobel prize, 1926)

Used Brownian motion to calculate
Avogadro number, $N_A (=R/k_B) \Rightarrow$
proved existence of molecules

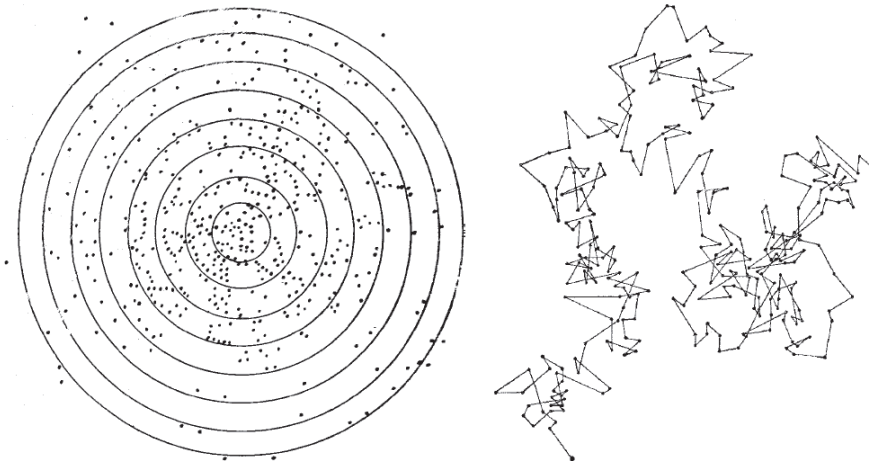
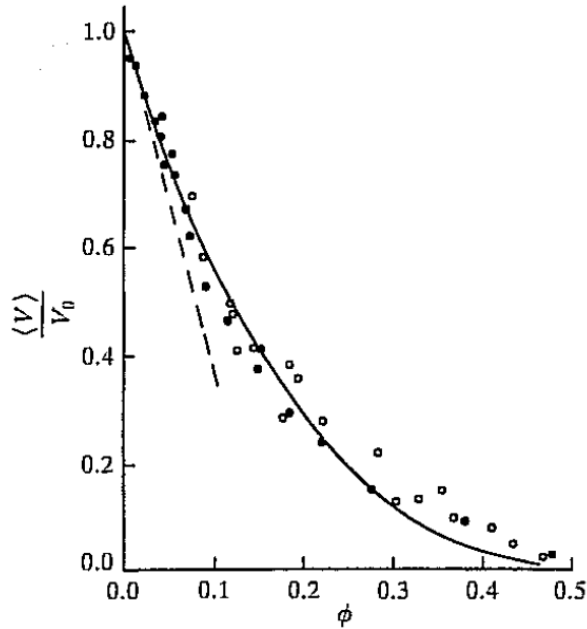


Figure 1.2. Jean Perrin's data, showing the location of colloidal particles released from the center at time zero and measured at time t . The right figure shows a typical trajectory of a $0.53 \mu\text{m}$ particle.



Main phenomena – Sedimentation



Sedimentation velocity

$$V_0 = \frac{2}{9} g R^2 \frac{\Delta \rho}{\eta}, \text{ isolated sphere}$$

For dilute concentrations $< \sim 10\% \Rightarrow$

Hydrodynamic interactions (two body) \Rightarrow slower sedimentation

$$\langle V \rangle = V_0 (1 - 6.55\phi), \quad \text{Batchelor (1972)}$$

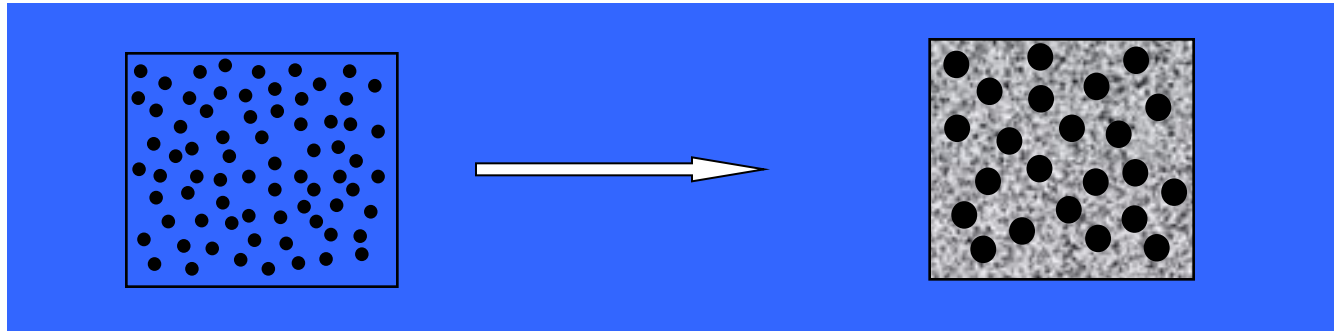
Large particles \Rightarrow Fast sedimentation

Deviations from Batchelor's prediction at higher $\phi \Rightarrow$

Multi-particle HI increase velocity



Colloidal systems – Time and length scales



Atomic

X1000

Colloidal

Time scales

Mechanical response

Length scale

$$\langle \Delta r(t)^2 \rangle = 6Dt$$

Slow

$$D = \frac{k_B T}{6\pi\eta R}$$

$$t \approx 1\text{ms} \dots 1\text{s}$$

$$G \propto \frac{k_B T}{R^3}$$

Soft

$d \approx \lambda$
(wavelength of light)

Stokes-Einstein-Sutherland diffusion

Large Enough =>
good for microscopy
and light scattering

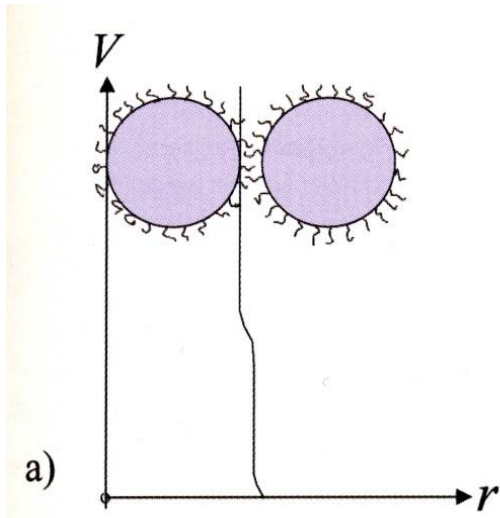
(Atomic: $t \approx 10^{-12} - 10^{-10}$ s)

$$G \approx 1 - 1000 \text{ Nm}^{-2}$$

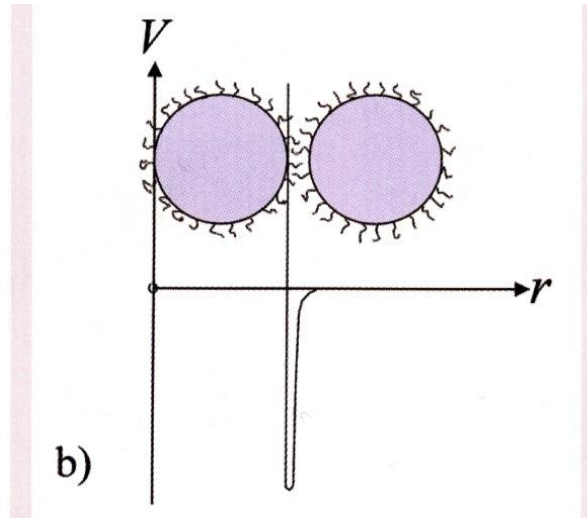
(Metals: $G \approx 10^9 - 10^{12} \text{ Nm}^{-2}$)



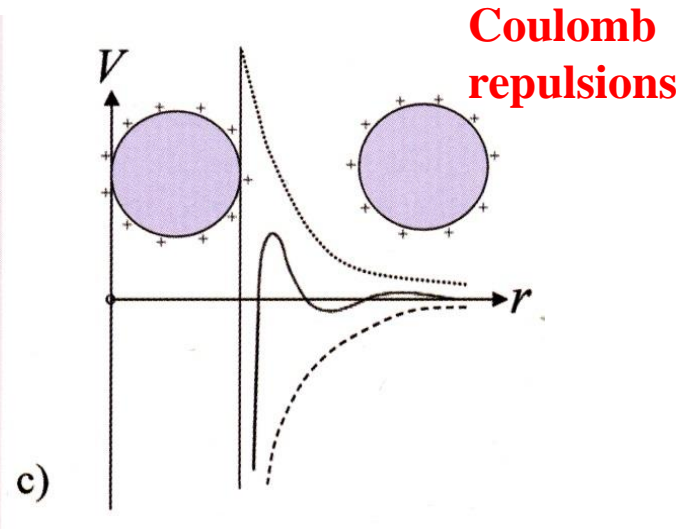
Forces - Interactions



nearly hard spheres



Attractive (sticky spheres)

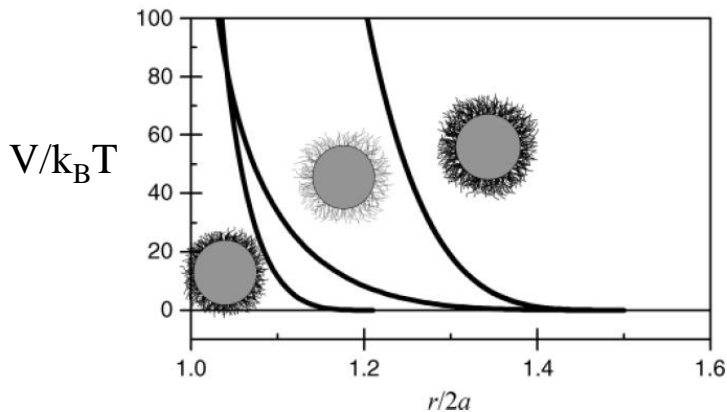


Coulomb repulsions

Van der Waals attractions

In bad solvent

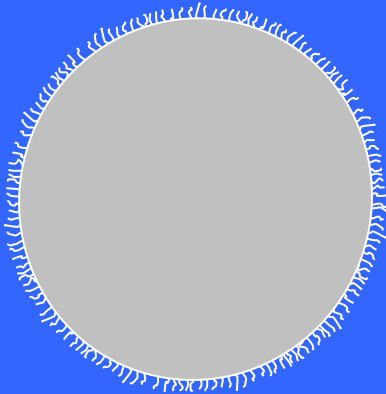
Charged colloids
(DLVO potential)



Sterically stabilized

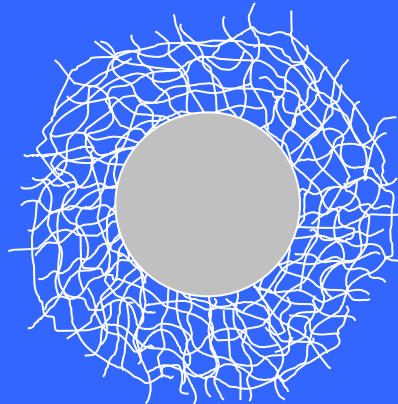


Repulsive colloids: From hard to soft interactions



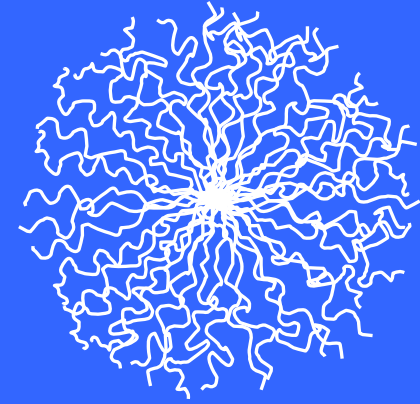
Hard spheres

(PMMA, silica particles etc.)

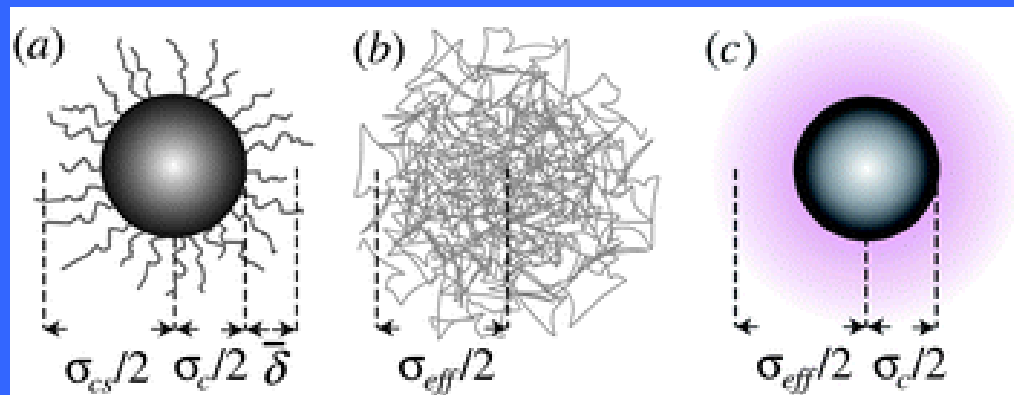


Core-shell microgels:

(example PS-PNIMAM)



**Ultra soft multiarm
star polymers or
Star-like micelles**



Polymer grafted particles

Crosslinked microgels

Charged particles



Interactions



van der Waals forces (usually attractive)

London or dispersion forces between two induced (fluctuating) dipoles

Interaction between 2 individual dipoles

$$U_{vdW}(r) = -\frac{C}{r^6}, \quad \text{with } C = \frac{3}{4} \left(\frac{1}{4\pi\epsilon_0} \right)^2 \alpha^2 \hbar \omega$$

Integrating for colloidal particles

Interaction per unit surface, between 2 semi-infinite solid planes at distance H:

$$U_{vdW}(H) = -\frac{A}{12\pi H^2}, \quad \text{with } A = \pi^2 \rho^2 C, \text{ Hamaker constant (usually } A > 0)$$

Interaction between 2 spheres of radius R, at surface-surface distance H:

$$U_{vdW}(H) = -\frac{AR}{12H} \left[1 + \frac{3H}{4R} + 2 \frac{H}{R} \ln\left(\frac{H}{R}\right) \right], \quad \text{for } H \ll R$$

$$\text{or } U_{vdW}(r) = -\frac{16Aa^6}{9r^6}, \quad \text{for } r \gg R$$



Interactions

Charged particles



Screened Coulomb repulsions in the presence of counter-ions

Diffuse double-layer model of Gouy & Chapman

Interaction potential between 2 planes

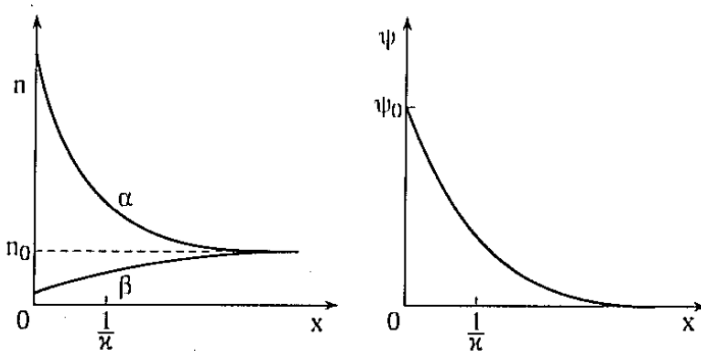
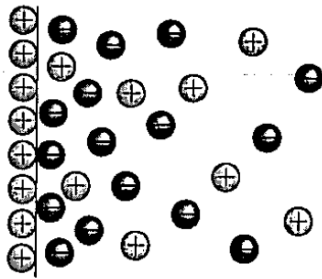
(semi-infinite solid planes):

$$U_{cb}(H) = \frac{64n_0k_B T}{\kappa} \tanh^2 \left(\frac{ze\psi_0}{4k_B T} \right) \exp(-\kappa H)$$

with n_0 the ion number density, z their valence, ψ_0 the surface potential,

and

$$\kappa^{-1} = \left(\frac{\epsilon\epsilon_0 k_B T}{2e^2 n_0 z^2} \right)^{1/2} \text{ the Debye Screening length}$$



Interaction potential between 2 spheres: $U_{cb}(H) = 2\pi\epsilon R\psi_0^2 \exp(-\kappa H)$ for $\kappa R < 5$



Interactions

Charged particles

Charged colloids – Total interaction potential

DLVO (Derjaguin, Landau, Verwey and Overbeek)

$$U_{DLVO}(\mathbf{r}) = U_{vdw}(\mathbf{r}) + U_{cb}(\mathbf{r})$$

Characteristics:

Primary/secondary minimum => irreversible/reversible aggregation

Repulsive barrier => particle stabilization

Increasing ion concentration <= e.g. addition of salt

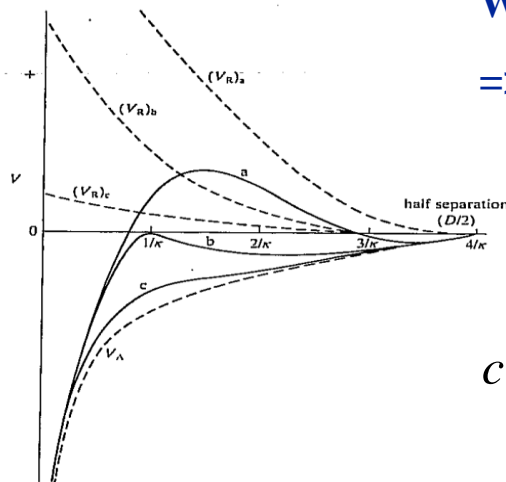
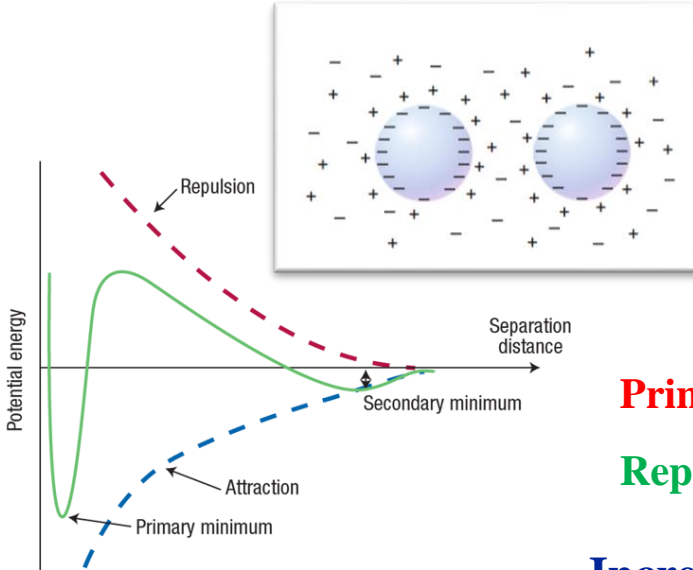


Weakening of repulsive interactions => decrease of Debye screening length

=> lowering of the repulsive barrier

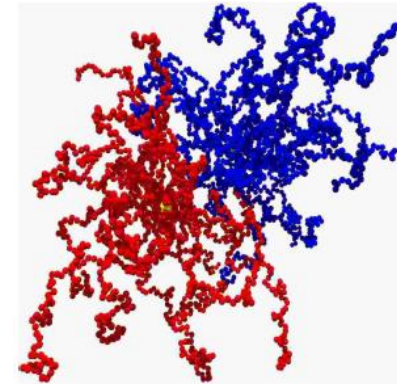
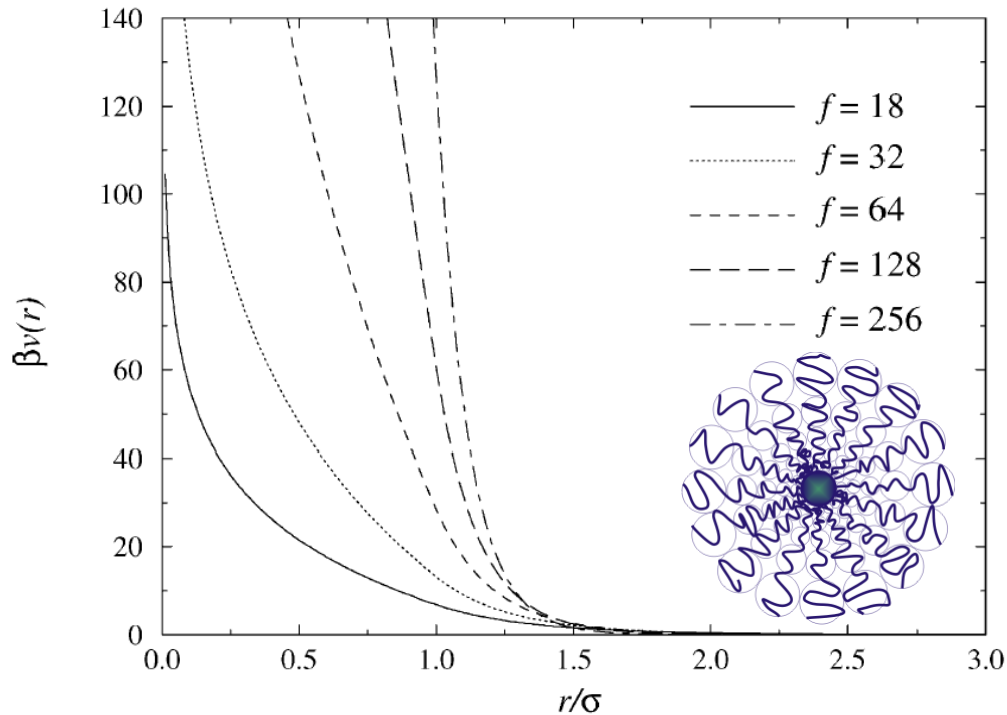
Barrier zero @ Critical coagulation concentration (ccc) :

$$c.c.c. [mol / lt] = \frac{(4\pi\epsilon_0\epsilon)^3 0.107 (k_B T)^5}{N_A A^2 (ze)^6} \tanh^4 \left(\frac{ze\psi_0}{4k_B T} \right)$$





Multiarm Star Polymers as model soft colloids



Parameters:

Functionality (number of arms) f

Molecular weight of arm M

Solvent quality

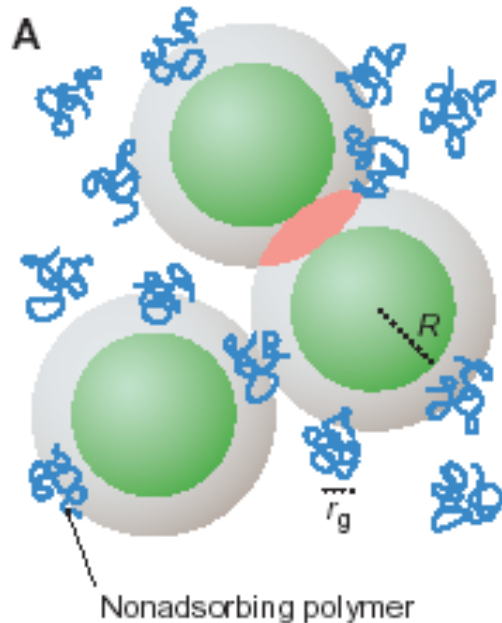
$$\frac{U(r)}{kT} = \begin{cases} (5/18) f^{3/2} \left[-\ln(r/\sigma) + (1 + \sqrt{f}/2)^{-1} \right] \\ (5/18) f^{3/2} (1 + \sqrt{f}/2)^{-1} (\sigma/r) \exp \left[-\sqrt{f}(r - \sigma)/2\sigma \right] \end{cases}$$



Depletion Interactions: Attractions in colloid-polymer mixtures

Induce attraction between the particles by adding non-adsorbing polymer chains

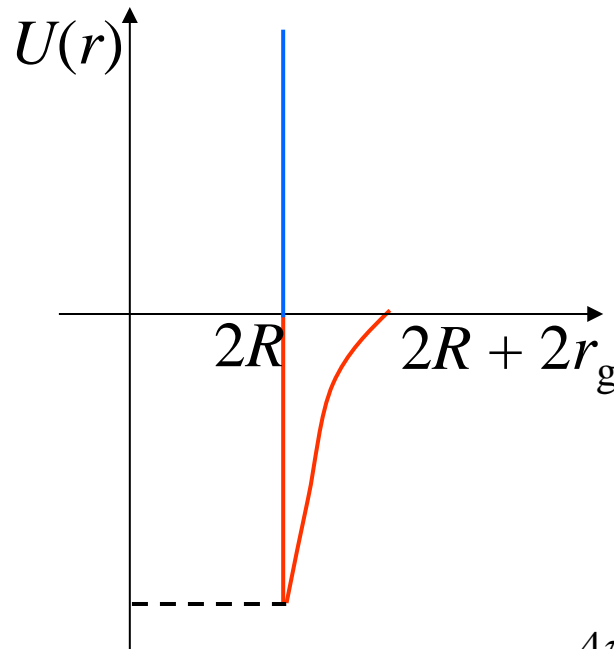
- “Depletion”:
- Unbalanced osmotic pressure pushes particles together
 - Overlap of depletion zones gives polymer more free volume (higher entropy)



Particle radius R

Polymer radius of gyration r_g

Overlap zone $L \sim r_g$



Can control

- range – size ratio r_g/R
- strength – polymer concentration

$$V_{ov} = \frac{4\pi}{3} (R+L)^3 \left(1 - \frac{3r}{4(R+L)} + \frac{r^3}{16(R+L)^3} \right)$$

$$\mathbf{F}_{dep} = -\mathbf{P}_{osm} \mathbf{V}_{ov} \quad \text{with} \quad P_{osm} = \frac{N}{V} k_B T$$

Asakura-Oosawa (AO) potential



Colloidal systems: Scale of main forces:

- **Gravitational:** $F_{gravity} \approx R^3 \Delta\rho g$
- **Brownian:** $F_{Brownian} \approx k_B T / R$
- **Electrostatic:** $F_{coulomb} \approx \epsilon \epsilon_0 \zeta^2$
- **Viscous (Stokes drag):** $F_{viscous} \approx \eta R v$
- **Van der Waals:** $F_{vdW} \approx A_{eff} / R^2$
- **Inertia:** $F_{inertia} \approx \rho R^2 v^2$

Example :

$$R = 1 \mu\text{m}, \eta = 1 \text{cp} = 10^{-3} \text{ Pa s}$$

$$\rho = 10^3 \text{ kg/m}^3, \Delta\rho/\rho = 0.01$$

$$T = 20^\circ \text{C}, v = 1 \mu\text{m/s}$$

$$A_{eff} = 10^{-20} \text{ Joule}, \zeta = 50 \text{ mV}$$

$$g = 10 \text{ m/s}^2, \epsilon = 100, \epsilon_0 = 8.85 \cdot 10^{-12} \text{ C/Vm}$$

ratios of forces:

$$\frac{F_{coulomb}}{F_{Brownian}} \approx 100$$

$$\frac{F_{vdW}}{F_{Brownian}} \approx 1$$

$$\frac{F_{viscous}}{F_{Brownian}} \approx 1$$

$$\frac{F_{gravity}}{F_{viscous}} \approx 0.1$$

$$\frac{F_{inertia}}{F_{viscous}} \approx 10^{-6}, (=Re)$$



Colloidal systems



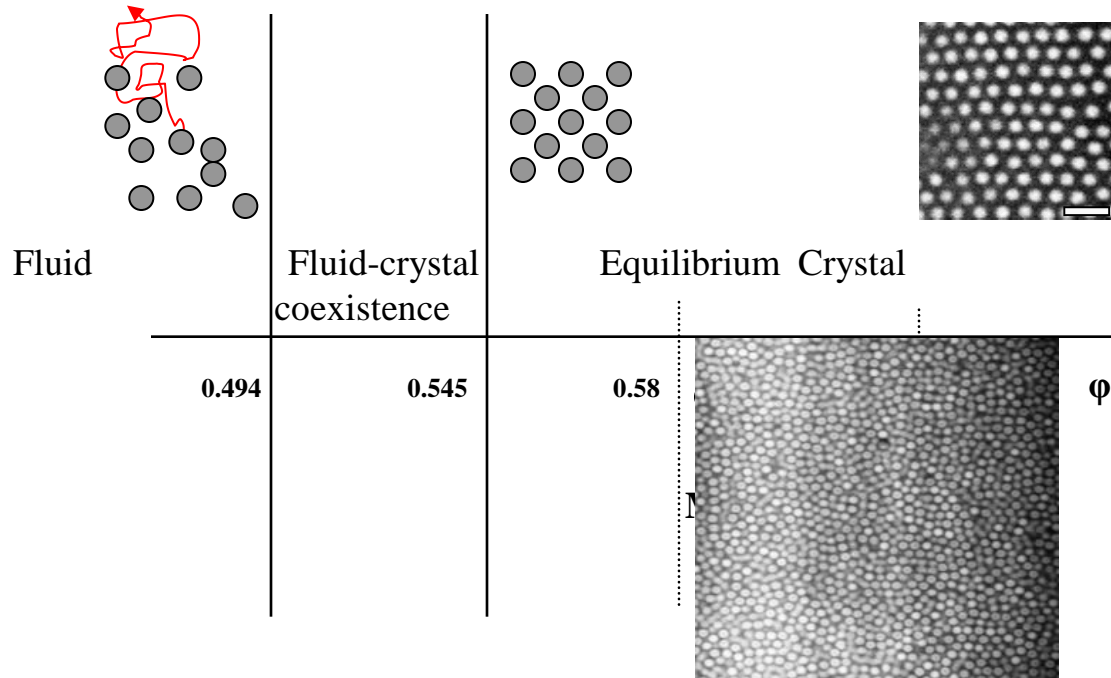
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- Microscopic Dynamics (Scattering-Microscopy)
- Mechanical properties (Rheology)

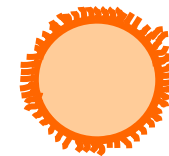


Phase behavior – Brownian Hard Spheres

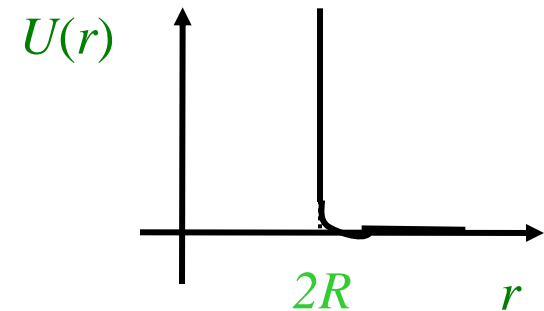
One-dimensional phase diagram



$$\phi = \frac{N}{V} \frac{4}{3} \pi R^3$$



PMMA spheres
Sterically stabilized
with PHSA



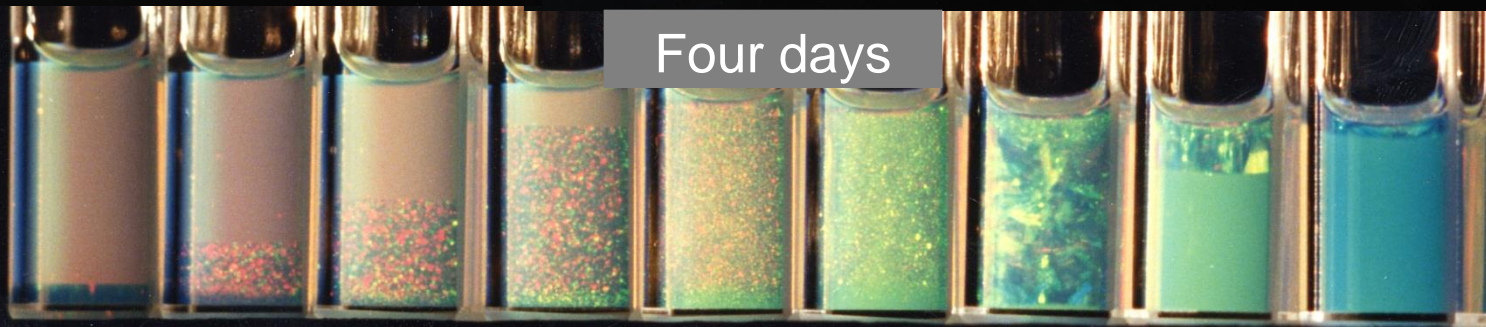
Entropy Driven Crystallisation

Crystal has *higher* entropy
than metastable fluid
at same concentration

Computer simulations:
Alder & Wainwright(1957)
Wood & Jacobson (1957)
Hoover & Ree (1968)

Experiments: Pusey, van Megen, Nature, 1986

Hard-sphere colloidal crystals and glasses



Fluid
 $\phi < 0.494$

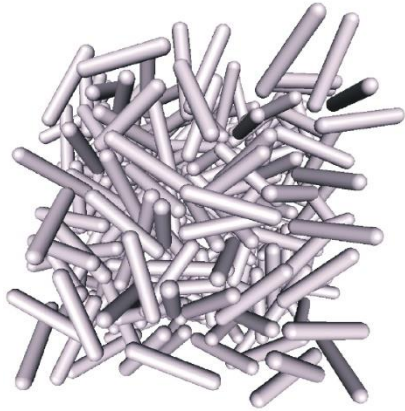
Fluid +
Crystal

Crystal
 $\phi > 0.545$

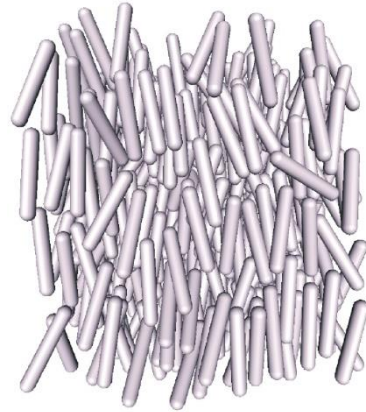
Glass
 $\phi > 0.58$



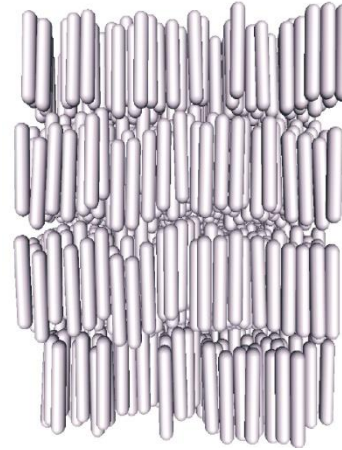
Other entropy driven transitions: Liquid crystals



Isotropic liquid



Nematic-liquid crystals



**Smectic-Liquid
Crystals**



Crystal



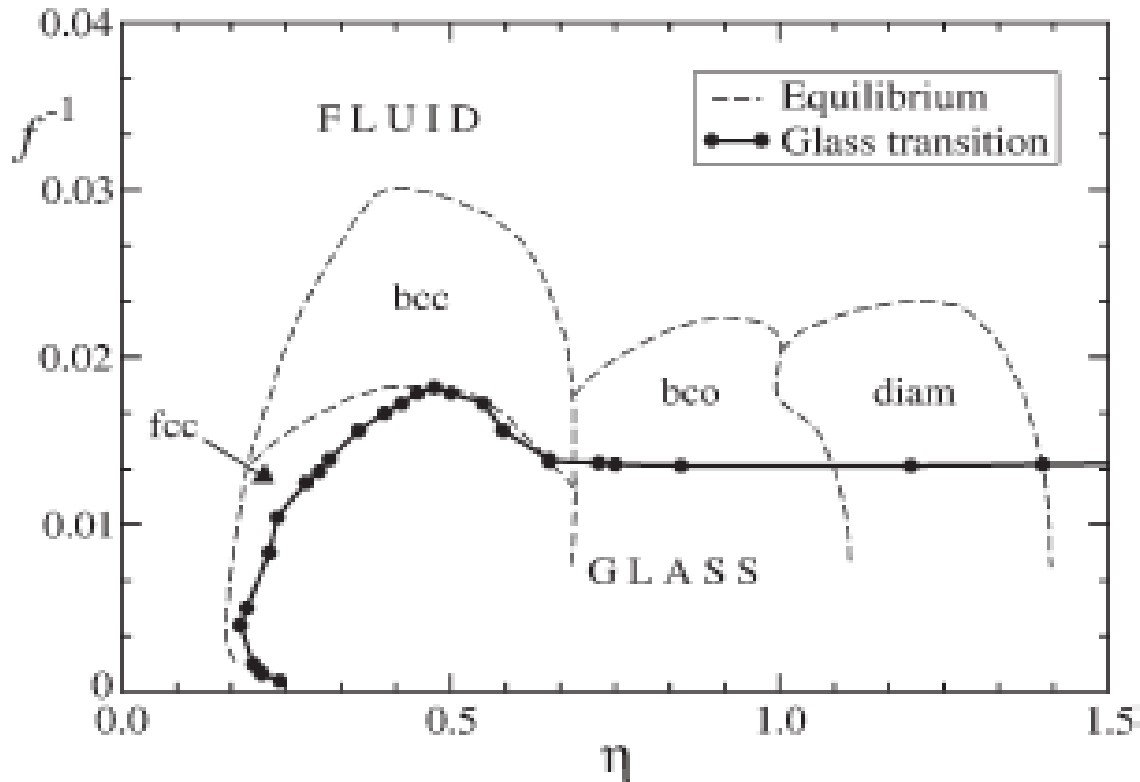
Decreasing temperature (thermotropic)

or increasing concentration (Lyotropic)

Entropy driven ordering: Isotropic-nematic transition in Hard rods



Phase behavior – Soft Multiarm Star colloids

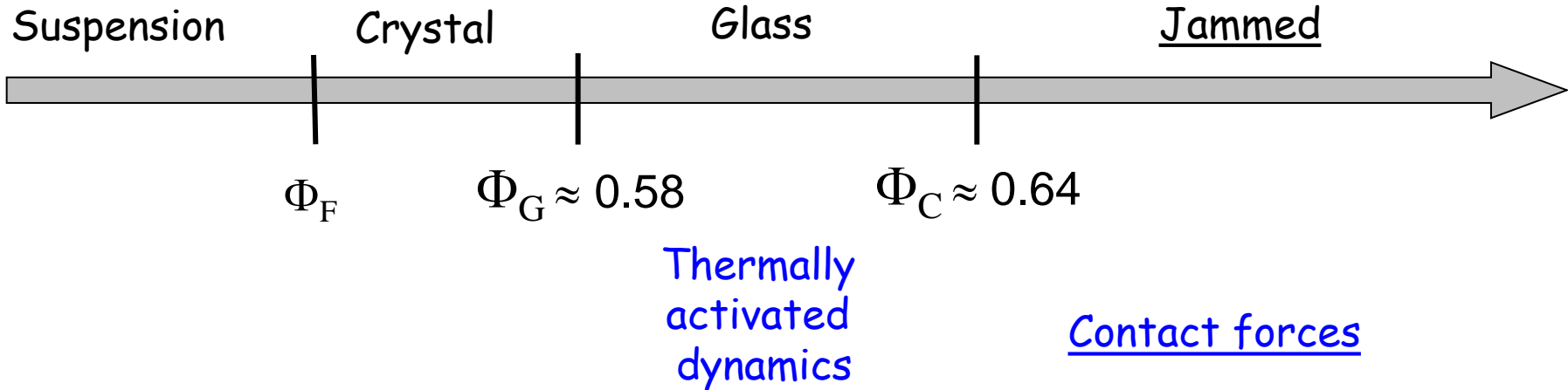
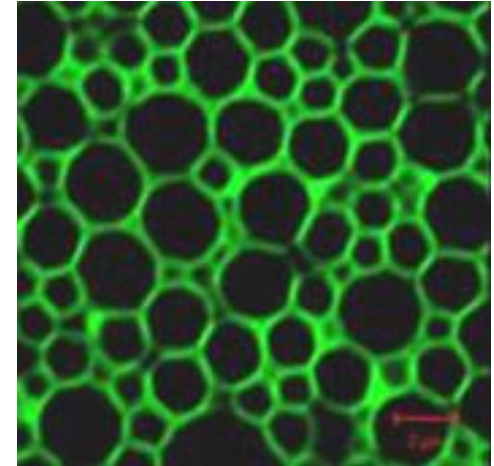
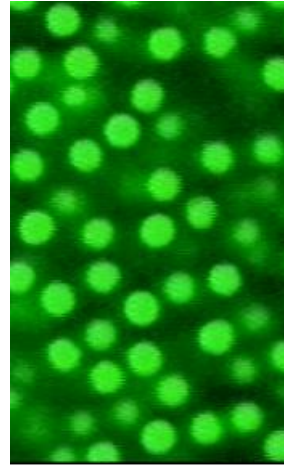
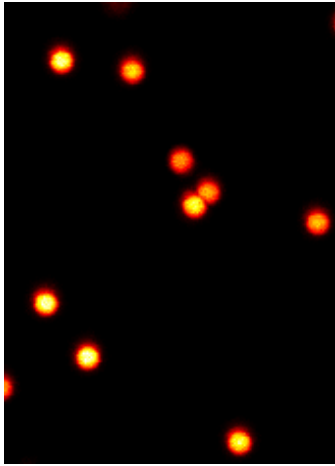


Watzlawek, PRL(1999), Foffi, PRL (2003)

Theoretical phase diagram: Liquid, crystal phases, glasses

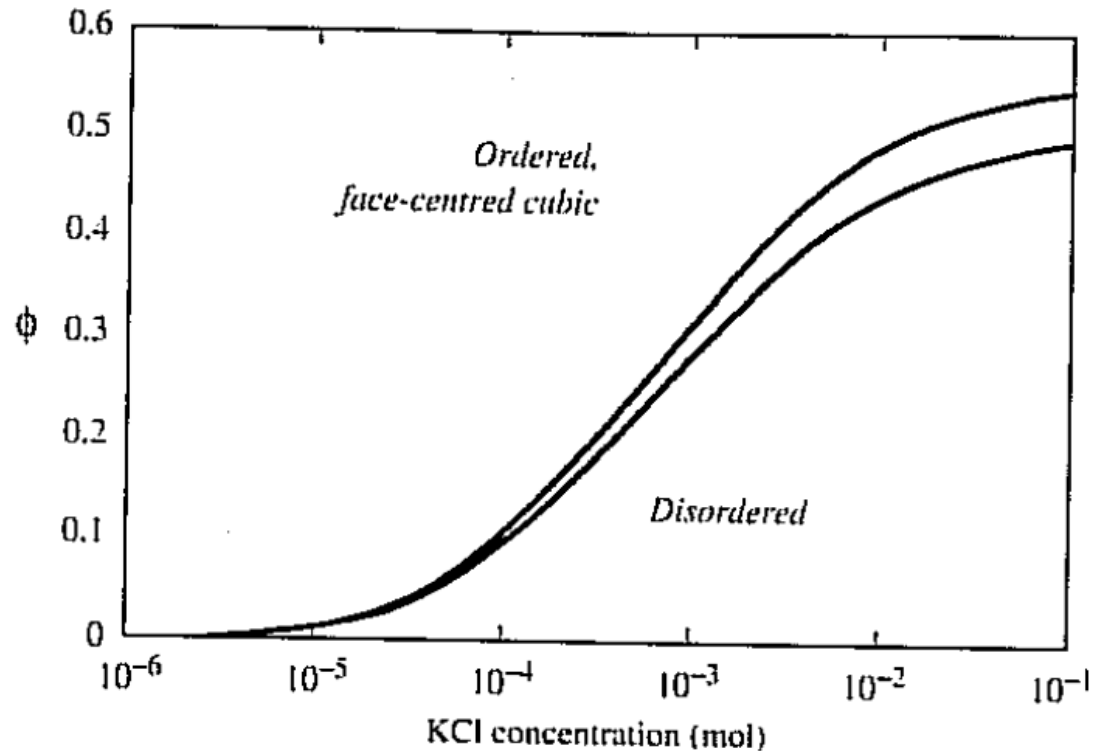


Phase behavior of repulsive colloids





Phase behavior – Charged colloids



Russel et al. (1989)

Long range repulsions =>

Liquid-crystal transition, coexistence and glassy states @ much lower ϕ than HSs

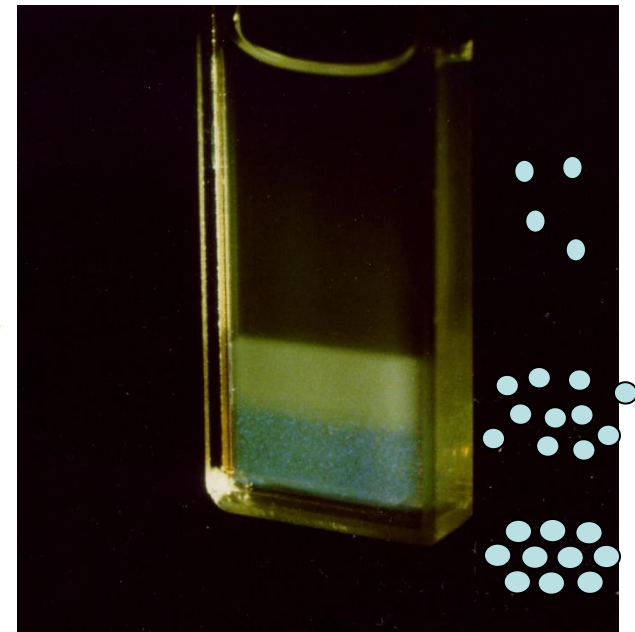
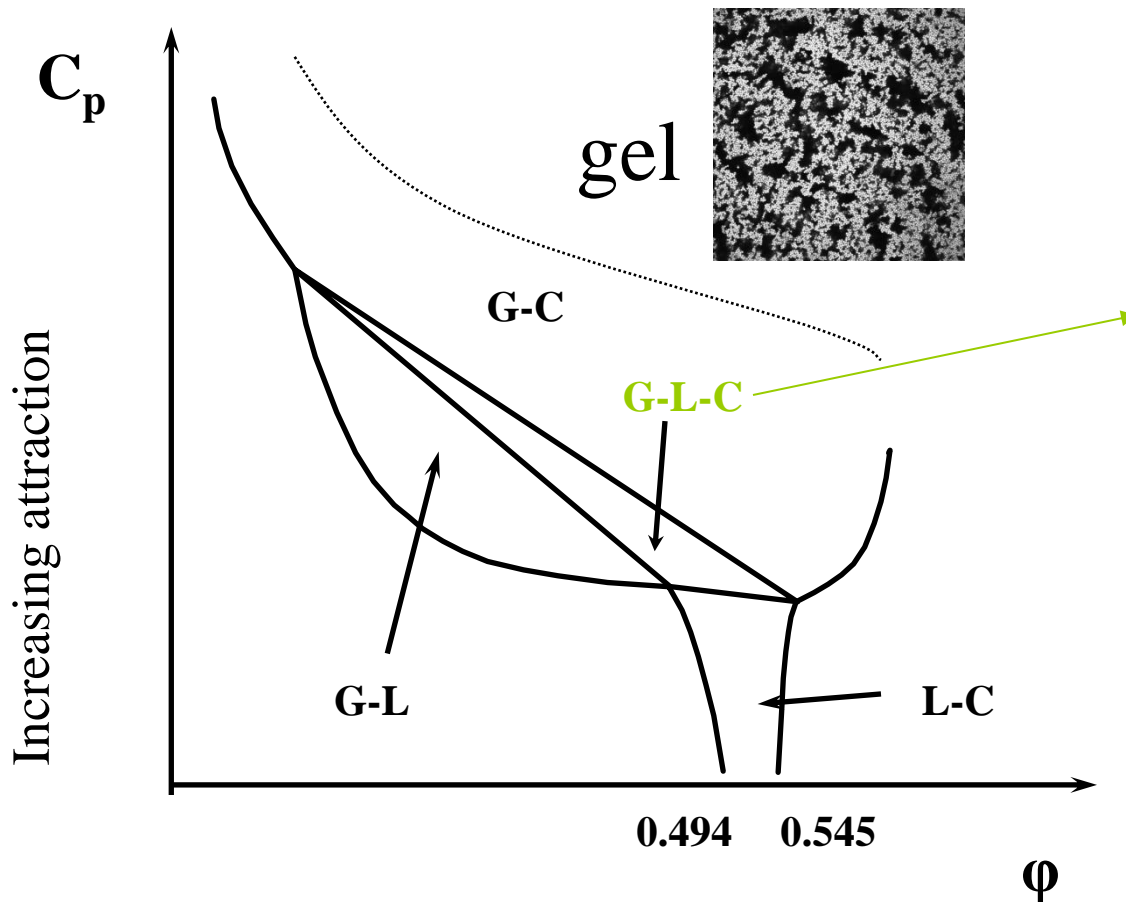


Phase diagram: Depletion attractions



Schematic experimental phase diagram (colloid-polymer mixtures)

For size ratio, $\xi > 0.25 \Rightarrow$ triple coexistence





Metastable states: Colloidal gels

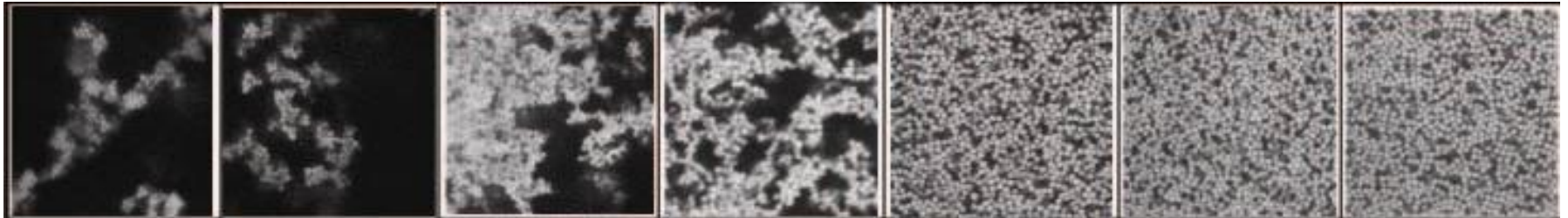


Increasing volume fraction

Free clusters

Interconnected networks

compact clusters -> attractive glass



Low volume fractions ($\varphi < 0.2$)
percolating network

Intermediate volume fractions (0.2-0.5):

Interplay with phase separation:
• Arrested phase separation
• or equilibrium gels

High volume fractions ($\varphi > 0.58$) => attractive glasses



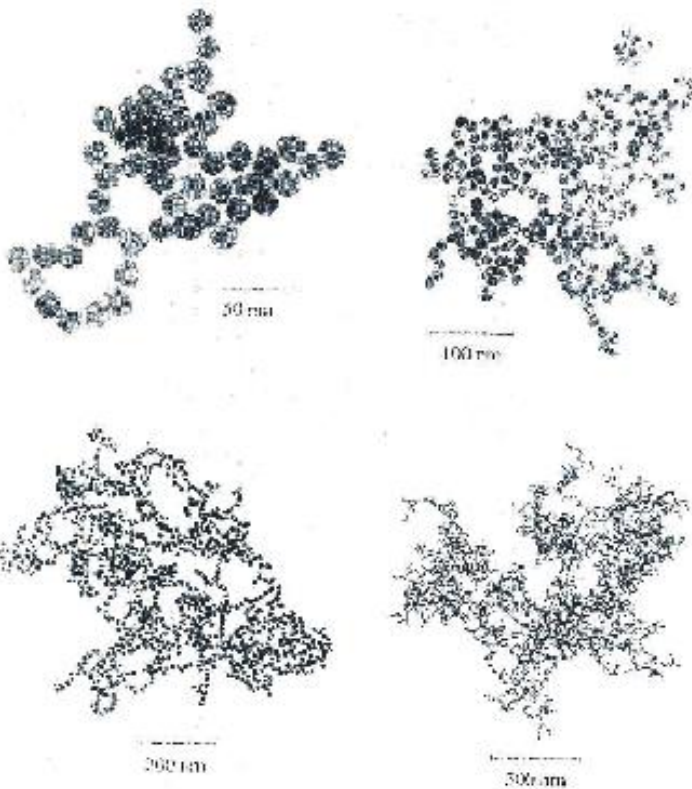
Low volume fractions: Fractal microstructure (flocs)



Aggregate structures in 3D and 2D

$$n \propto R^{d_f}$$

n = number of particles within distance R from center of floc
 d_f = fractal dimension



High attraction strength =>

Diffusion Limited aggregation

(DLCA): $d_f = 1.7-1.8$

Low attraction strength =>

Reaction Limited aggregation

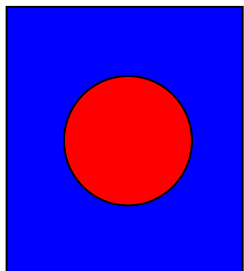
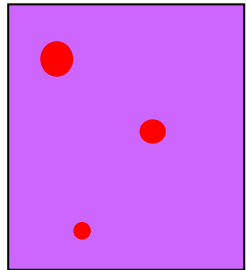
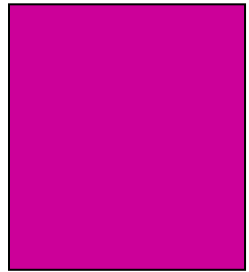
(RLCA): $d_f = 2.0-2.1$



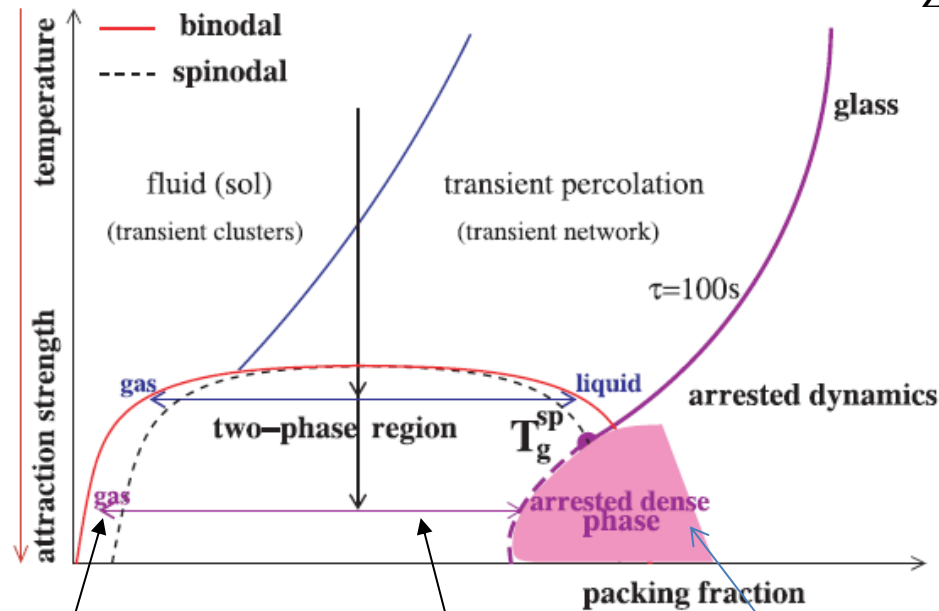
Phase transition – gelation kinetics



Zaccarelli, JPCM, 2007



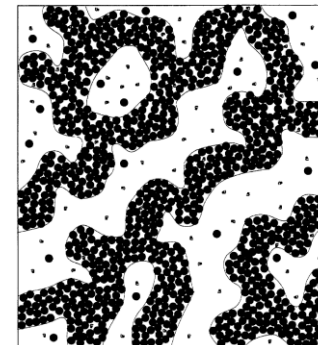
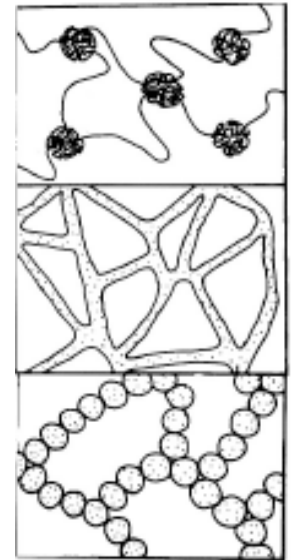
Metastable:
Nucleation
& growth



Schematic for long(er)
range attractions

Gels through
Arrested phase
separation

Unstable:
Spinodal
decomposition



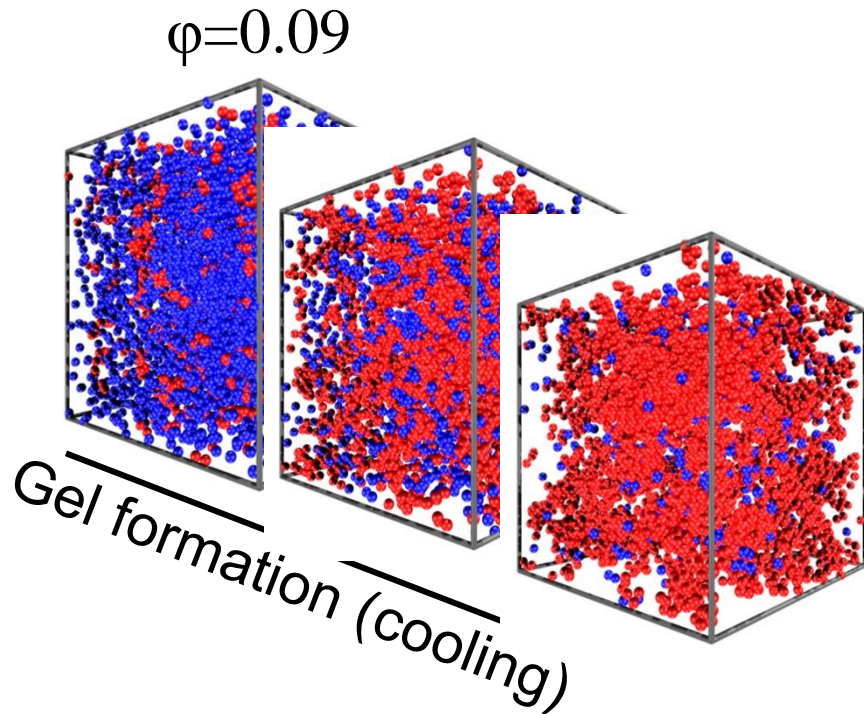
Verhaegh et al.
Physica A



Evolution of structure during gelation



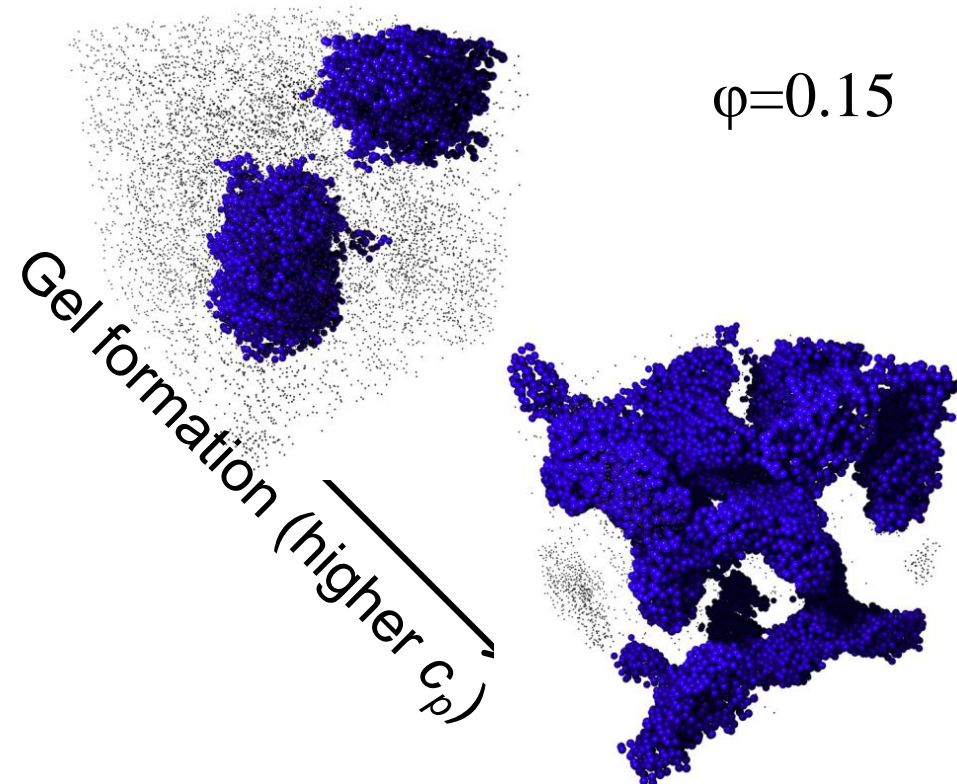
**adhesive hard-spheres (AHS)
(one component)**



Snapshots courtesy of Castañeda-Priego

Macroscopically percolated
homogenous structure

(Wagner+Mewis)
**Colloid-polymer mixture
(two components)**



Figures from Liu et al., PRL 96 (2006)

Heterogeneous structure that is
arrested due to attraction



Metastable states: Colloidal gels



Ageing => coarsening of colloidal gel with waiting time

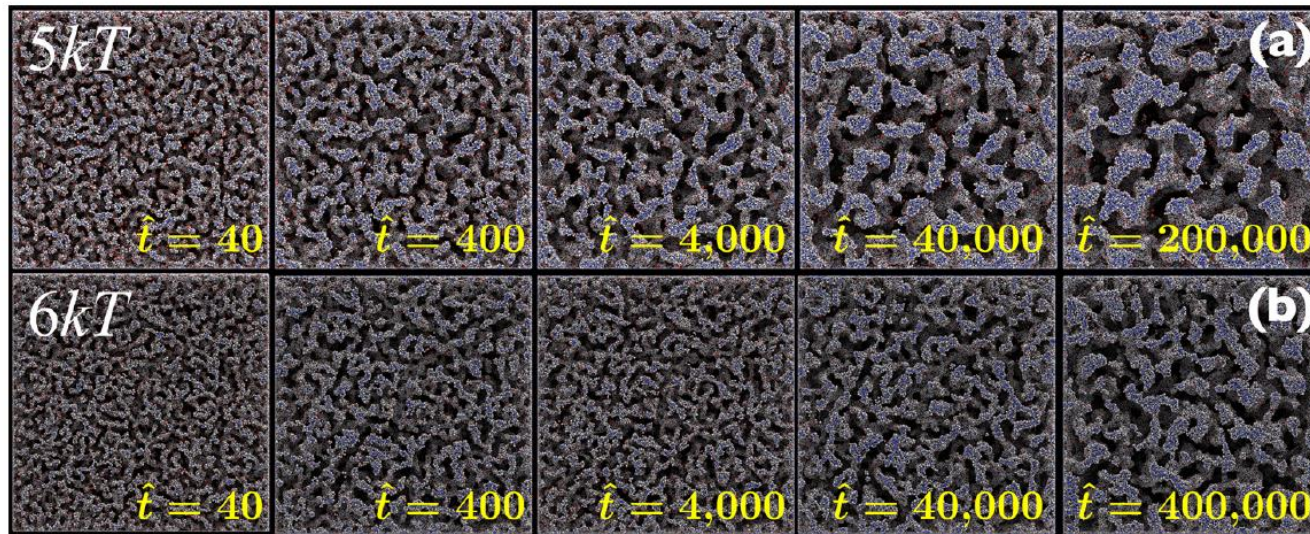


FIG. 5. Evolution of particle microstructure over time for (a) top row, $5 kT$ gel and (b) bottom row, $6 kT$ gel. The gel in each snapshot is older than the previous image as indicated.

Brownian Dynamics simulations, $\phi=0.2$,



Colloidal systems



Outline:

- Definitions-Examples-Applications
- Main phenomena – Forces - Time scales
- Phase behavior: Thermodynamic phases, Metastable states (glasses and gels)
- **Microscopic Dynamics (Scattering-Microscopy)**
- Mechanical properties (Rheology)



Microscopic Structure and Dynamics

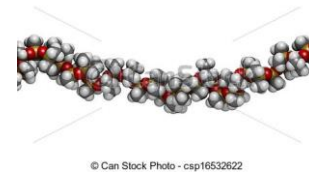
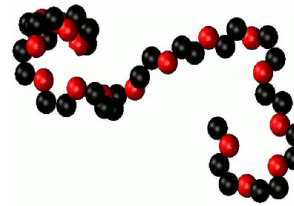
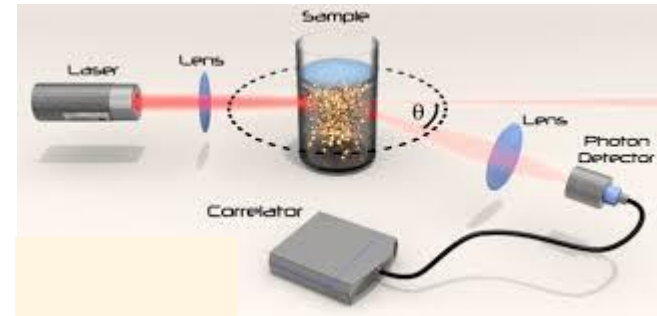


Light scattering (reciprocal space)

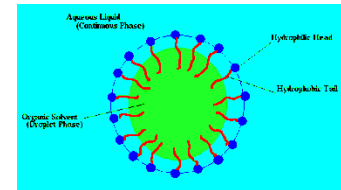
Probe fluctuations at scattering wave vector q .

$$q = 4\pi n/\lambda \sin(\theta/2)$$

Measure structure and particle dynamics of polymers, colloids, emulsions



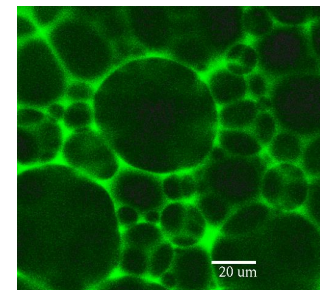
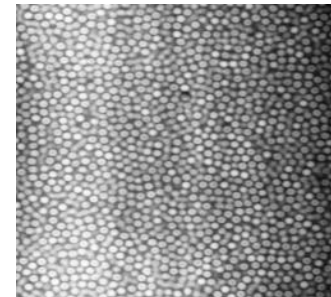
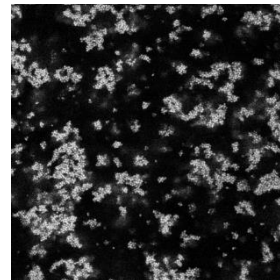
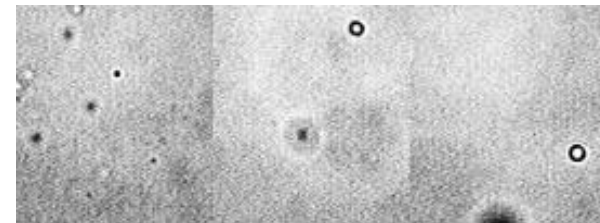
© Can Stock Photo - csp16532622



Optical Microscopy (direct space)

Measure structure and particle dynamics

State of the art: Fast fluorescence confocal microscopy follow dynamics also under shear

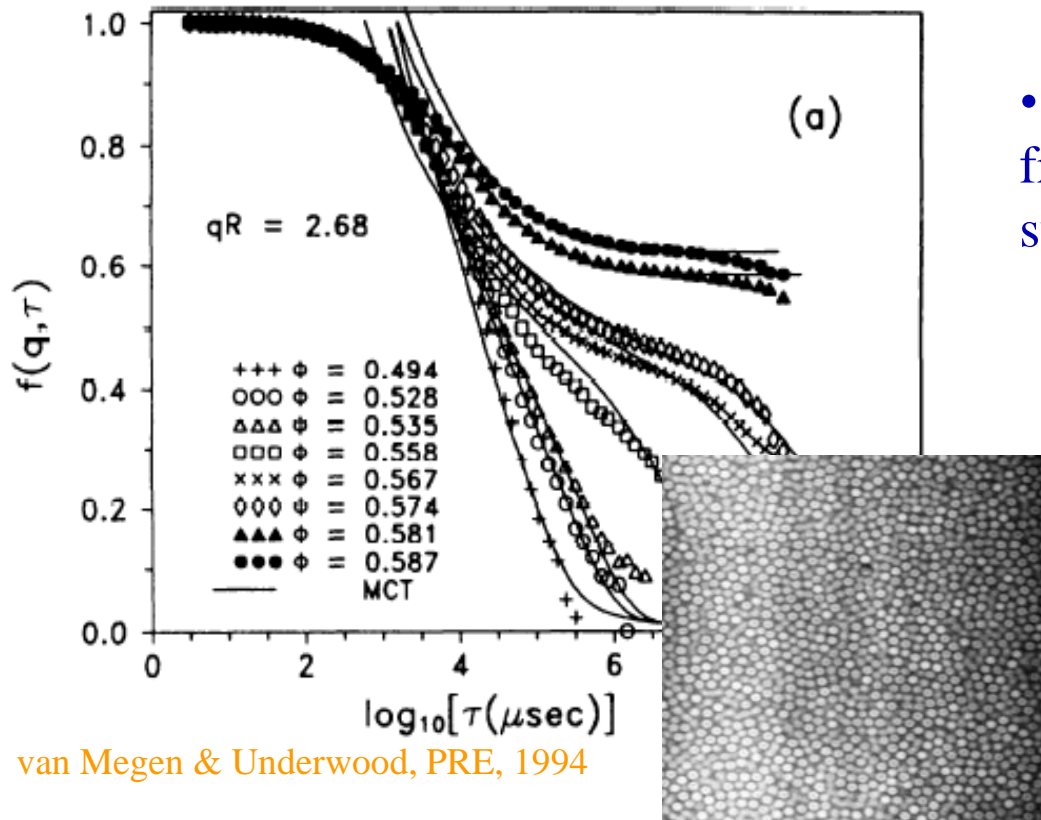




Dynamics: colloidal Suspensions



DLS for HS's at $0.49 < \phi < 0.59$



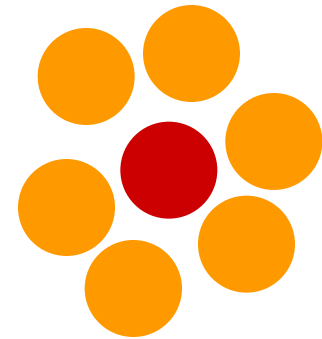
van Meegen & Underwood, PRE, 1994

$$f(q, t) = \frac{1}{N} \sum_{j=1}^N \sum_{i=1}^N \langle \exp(i\bar{q} \cdot (\bar{r}_i(0) - \bar{r}_j(t))) \rangle$$

$$q = 4\pi n / \lambda \sin(\theta/2)$$

• As ϕ increases the particles are caged more and more

• At $\phi \sim 0.58$, fluctuations partly freeze and crystallization is suppressed



Mode Coupling Theory (MCT)

predicts a transition to a
dynamically
arrested non-ergodic state

(repulsive glass)

Götze 1980

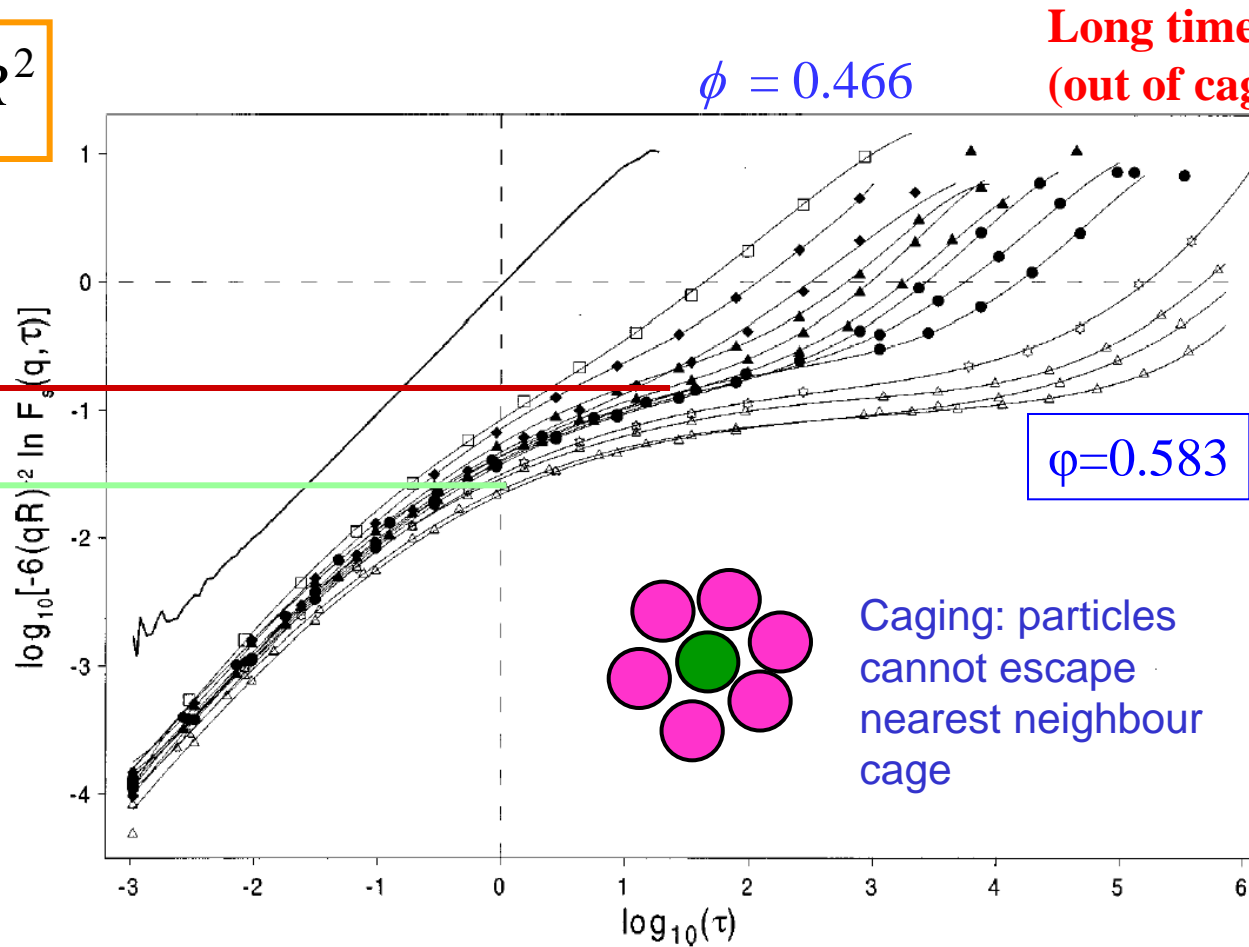


Mean Square displacement

$$\langle \Delta r^2(t) \rangle / R^2$$

$$\sqrt{\langle \Delta r^2(t) \rangle} \cong 0.28R$$

$$\sqrt{\langle \Delta r^2(t) \rangle} \cong 0.16R$$



Short time dynamics
(in-cage)

Long time dynamics
(out of cage)

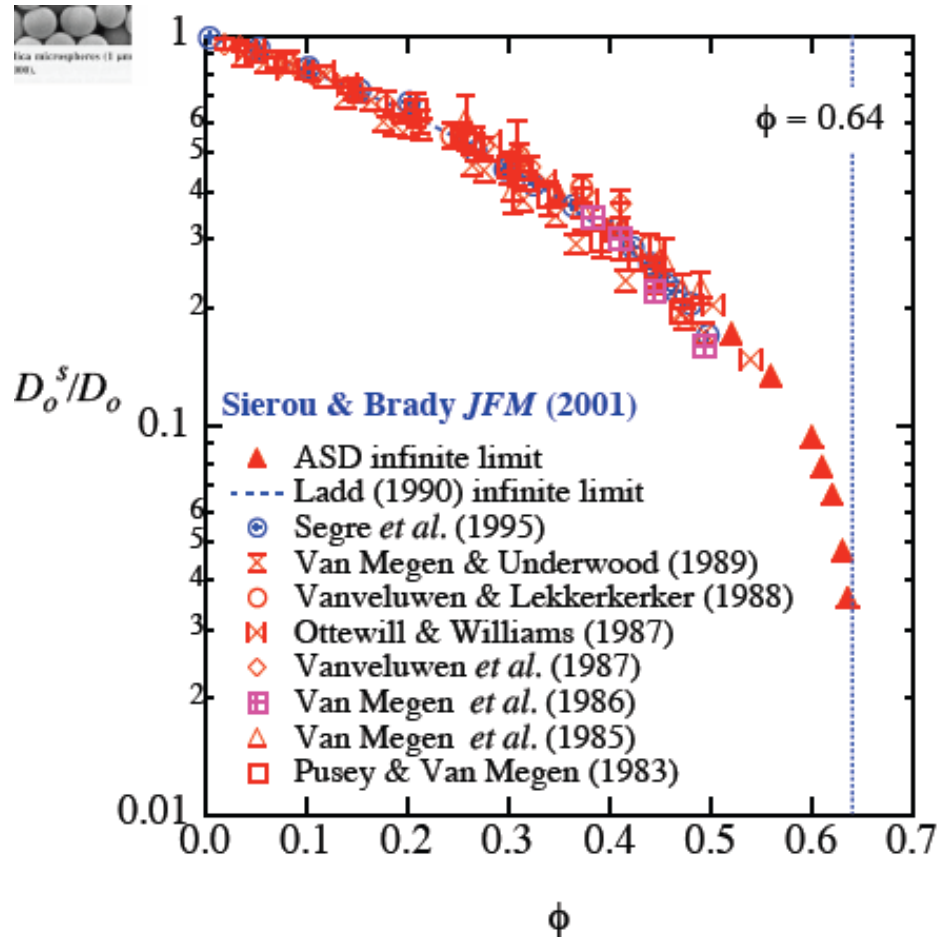
(Van Meegen, PRE, 1999)



Hard Spheres: Short-time self diffusion



Volume fraction dependence



Batchelor's prediction

Hydrodynamic effect at low ϕ ,

(pair wise contributions)

Dilute limit: $\phi \rightarrow 0$

$$D_o^s(\phi) \sim D_o(1 - 1.83\phi)$$

Close packing:

$$\varepsilon = 1 - \phi/\phi_{rcp} \rightarrow 0$$

$$D_o^s(\phi) \sim D_o/\ln(1/\varepsilon)$$

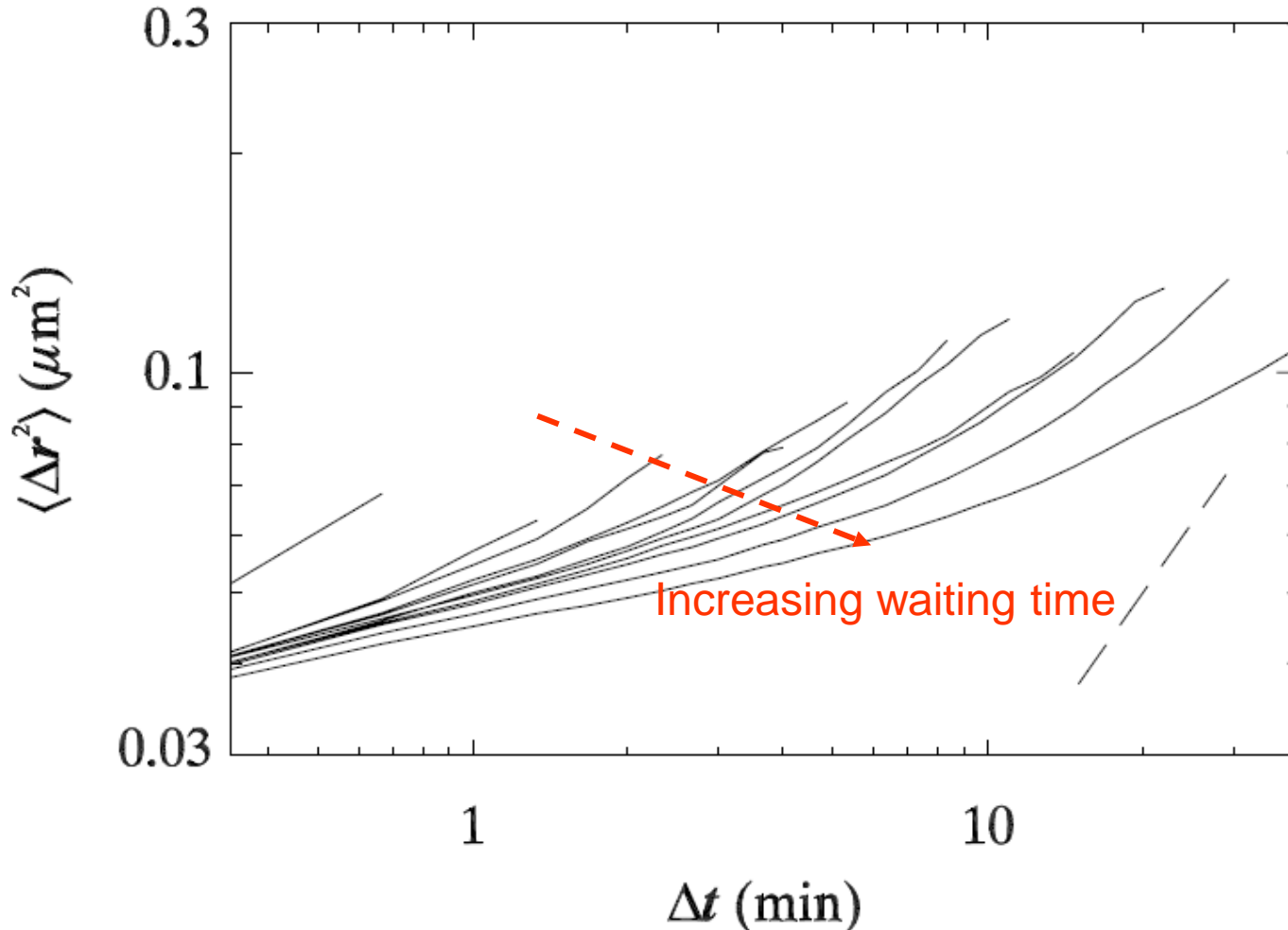
In-cage diffusion decrease towards zero @ rcp ($\phi=0.64$)



Ageing of the hard-sphere glass



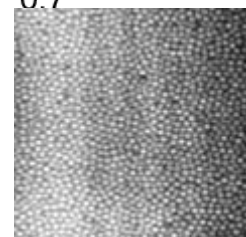
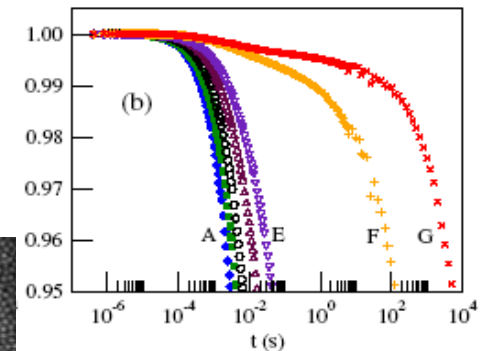
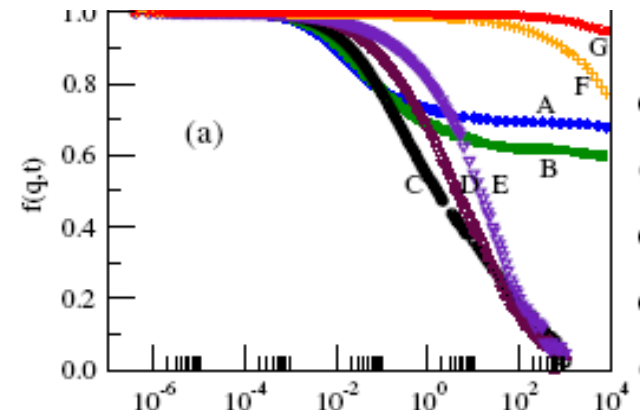
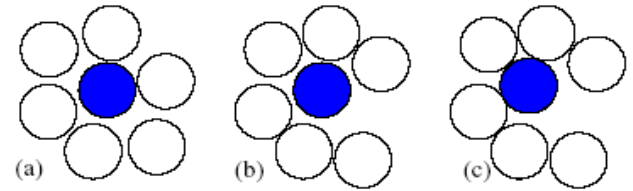
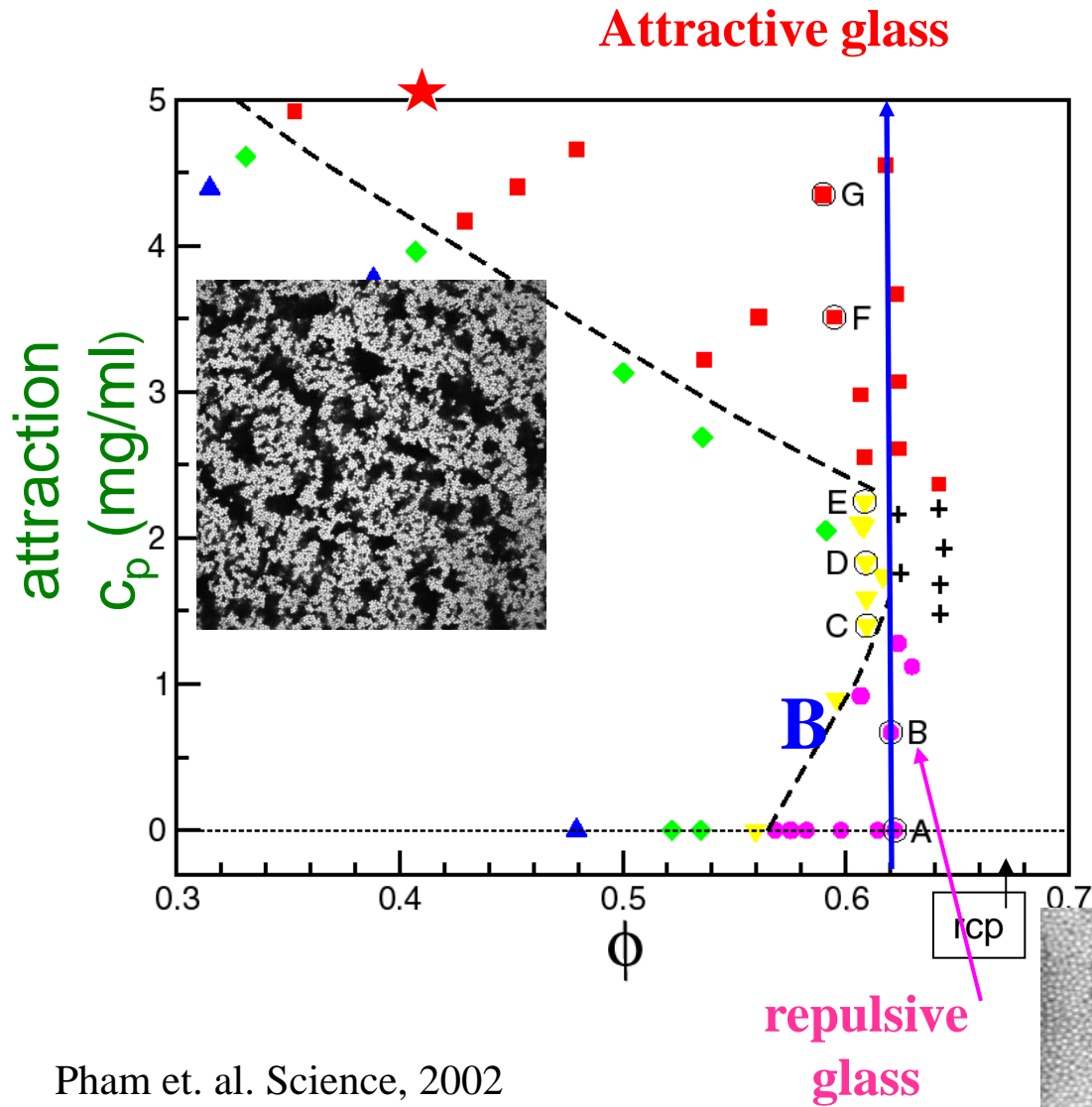
Long-time (out of cage) dynamics slow down with waiting time near the glass transition



Courtland & Weeks, *JPCM* **15** S359, confocal particle tracking



Re-entrant glass transition: repulsive to attractive glass

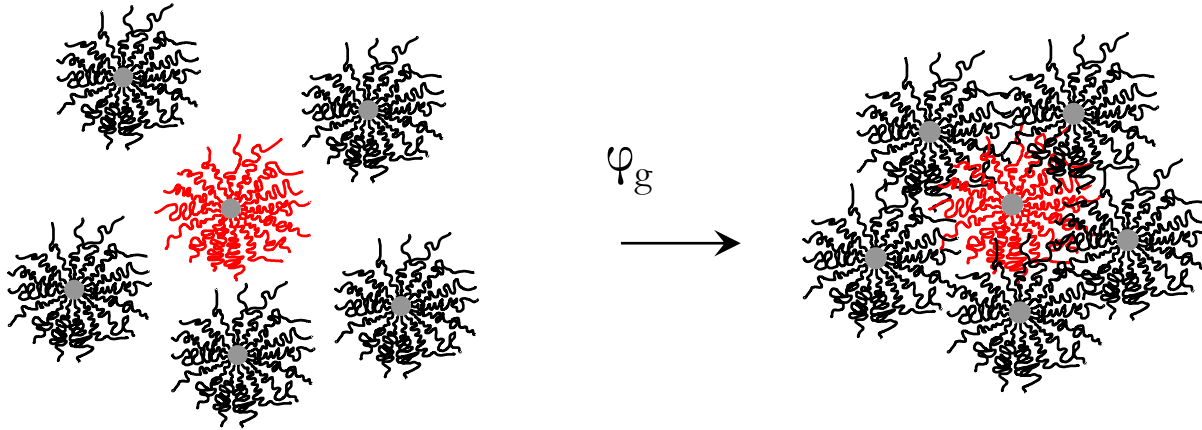




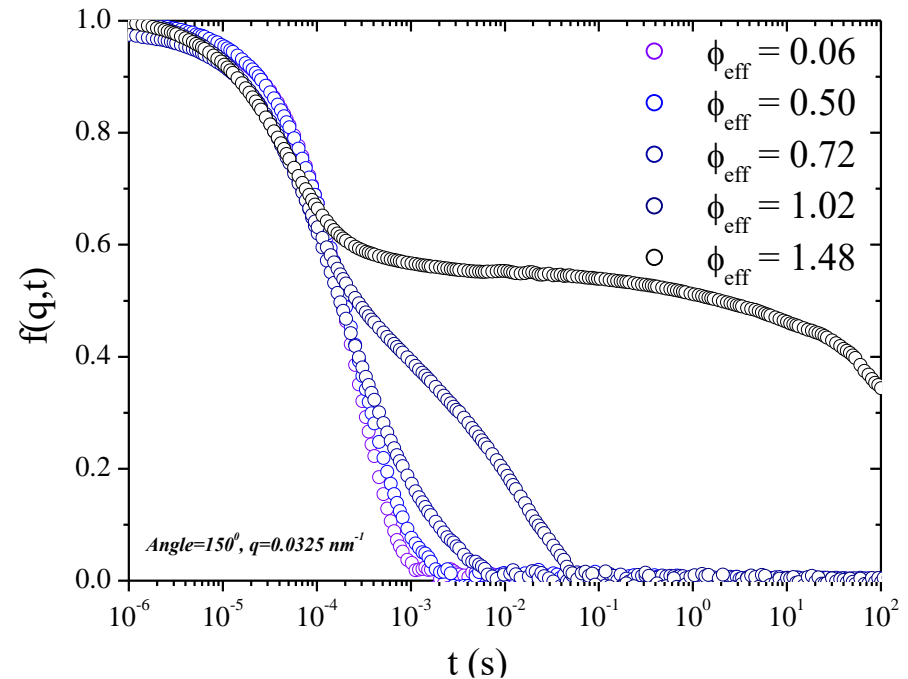
Soft Colloids - Dynamics approaching the glass



Multiarm Stars



Caging with increasing c or T





Colloidal systems



END of Lecture 1

- Definitions-Examples-Applications
- Main phenomena – Forces - Time scales
- Phase behavior: Thermodynamic phases, Metastable states (glasses and gels)
- Microscopic Dynamics (Scattering-Microscopy)
- **Mechanical properties (Rheology) => lecture 2**



Colloidal systems



Study questions (Lecture 1)

1. Define colloidal systems. Why are colloidal particles defined by size limitations from nanometers to micrometers?
2. What is the phase diagram of hard spheres, and how is it changed for soft polymer coated particles?
3. What is the role of a polymer in colloidal dispersion stability for a) Grafted or adsorbed polymer b) Dissolved, non-adsorbed polymer?
4. Describe the interaction potential and the phase diagram of charged stabilized colloids.
5. Calculate the van der Waals interaction per unit area between two semi-infinite planes.
6. Determine the critical coagulation concentration (c.c.c) (in mol/L) for two planar surfaces (*use approximately the vdW and screened Coulomb interaction between semi-infinite planes*)
7. Calculate the time needed for a colloidal particle with radius, $R=0.5 \mu\text{m}$ to diffuse its own diameter in water at 25 °C in the dilute limit and at a volume fraction of $\phi=0.1$
8. Calculate the sedimentation velocity of a particle with $R=2\mu\text{m}$ and $\rho=1.2\text{g/cm}^3$ in the dilute limit and at $\phi=0.05$ and 0.3.
9. A colloidal glass of hard spheres with $R=100 \text{ nm}$, at $\phi=0.6$ has $G'=80 \text{ Pa}$ at $\omega=10 \text{ rad/s}$ and $T=20 \text{ }^\circ\text{C}$. Calculate the G' for a glass at the same ϕ in the case of HS with $R=500 \text{ nm}$ at $T=40 \text{ }^\circ\text{C}$. At which frequency ω we should make the comparison?
10. Calculate the ratio of main forces in a colloidal suspension with:

$$R = 1 \mu\text{m}, \eta = 1 \text{cp} = 10^{-3} \text{ Pa s}, \rho = 10^3 \text{ kg/m}^3, \Delta\rho/\rho = 0.01, T = 20^\circ\text{C}, v = 1 \mu\text{m/s}, A_{\text{eff}} = 10^{-20} \text{ Joule}, \zeta = 50 \text{ mV}$$
$$g = 10 \text{ m/s}^2, \varepsilon = 100, \varepsilon_0 = 8.85 \cdot 10^{-12} \text{ C/Vm}$$



Colloidal systems



Study questions cont. (Lecture 1)

11. You are trying to flocculate a colloidal dispersion in a plant-size operation at 500 K using calcium oxide (CaO). In your laboratory, all you have available at the moment is sodium chloride (NaCl). At room temperature, you find that 2 mol/L NaCl is necessary to induce flocculation. Estimate the concentration of CaO necessary to flocculate the dispersion in your plant operation.
12. Determine the crystal-liquid coexistence regime for charged stabilized particles with a Debye screening length $1/\kappa = 10$ nm and radius $R = 150$ nm. Assume the particles behave as hard spheres with an effective radius $R + 1/\kappa$.
13. What is the difference between the behavior of power law fluids and Bingham bodies at low stress levels?
14. Can you rationalize the dependence of the Debye screening length on the thermal energy, and ion concentration?
15. What is a colloidal glass, a colloidal gel and an attractive glass?



Colloidal systems



Further reading (Lecture 1)

Books:

- W.B. Russel, D.A. Saville, W.R.Schowalter, Colloidal Dispersions, Cambridge University Press, 1989
- R. J. Hunter, Foundations of Colloid Science, Oxford, University Press, New York, 2001
- D. F. Evans, H. Wennerström, The Colloidal Domain, Where Physics, Chemistry, Biology and Technology meet, John Willey and Sons, New York, 1999.
- M.D. Haw “Middle World: The Restless Heart of Matter and Life”, 2006

Reviews:

- P.N. Pusey, in Les Houches Session 51, ed. D. Lesvesque, J. P. Hansen and J. Zinn-Justin, North-Holland, Amsterdam, (1991).
- W. C. K. Poon, J. Phys.: Condens. Matter, (2002), 14, R859–R880.
- C. N. Likos, Physics Reports 348, (2001) 267-439